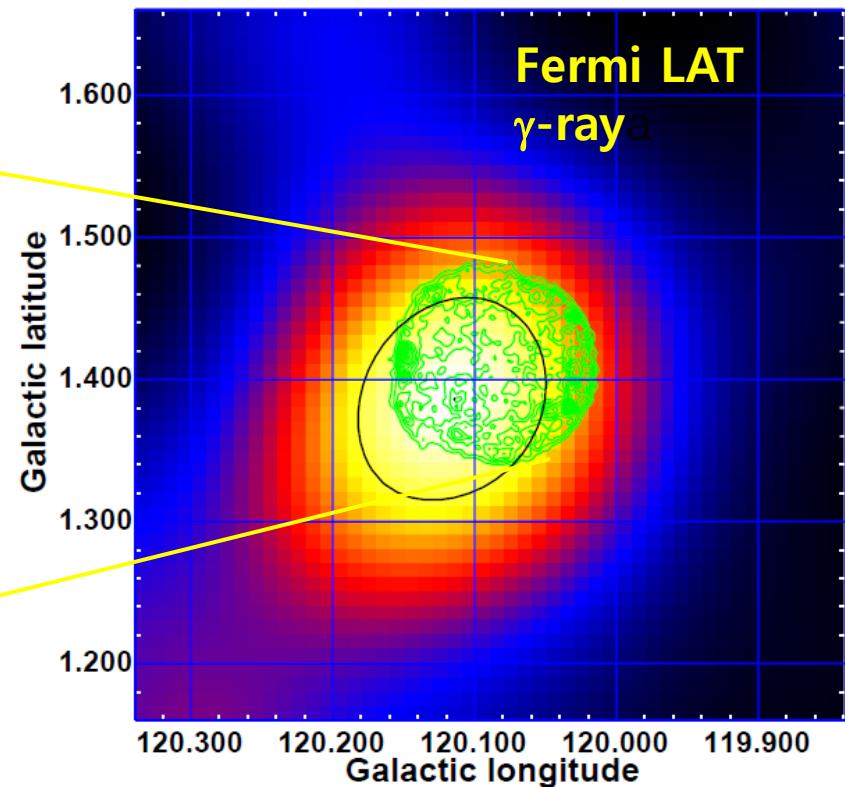
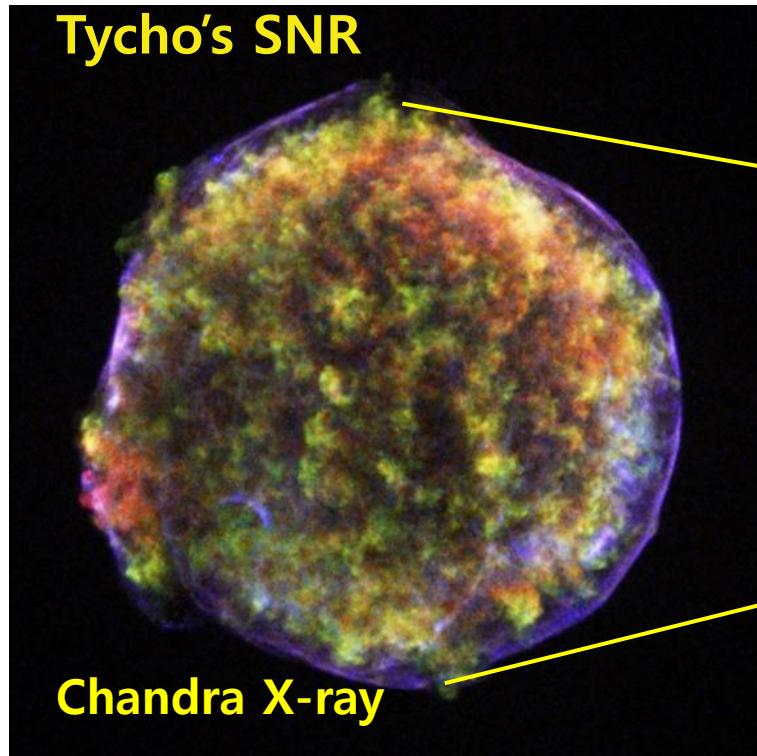


Problems in Estimating Non-thermal Radiation from Supernova Remnants

Hyesung Kang

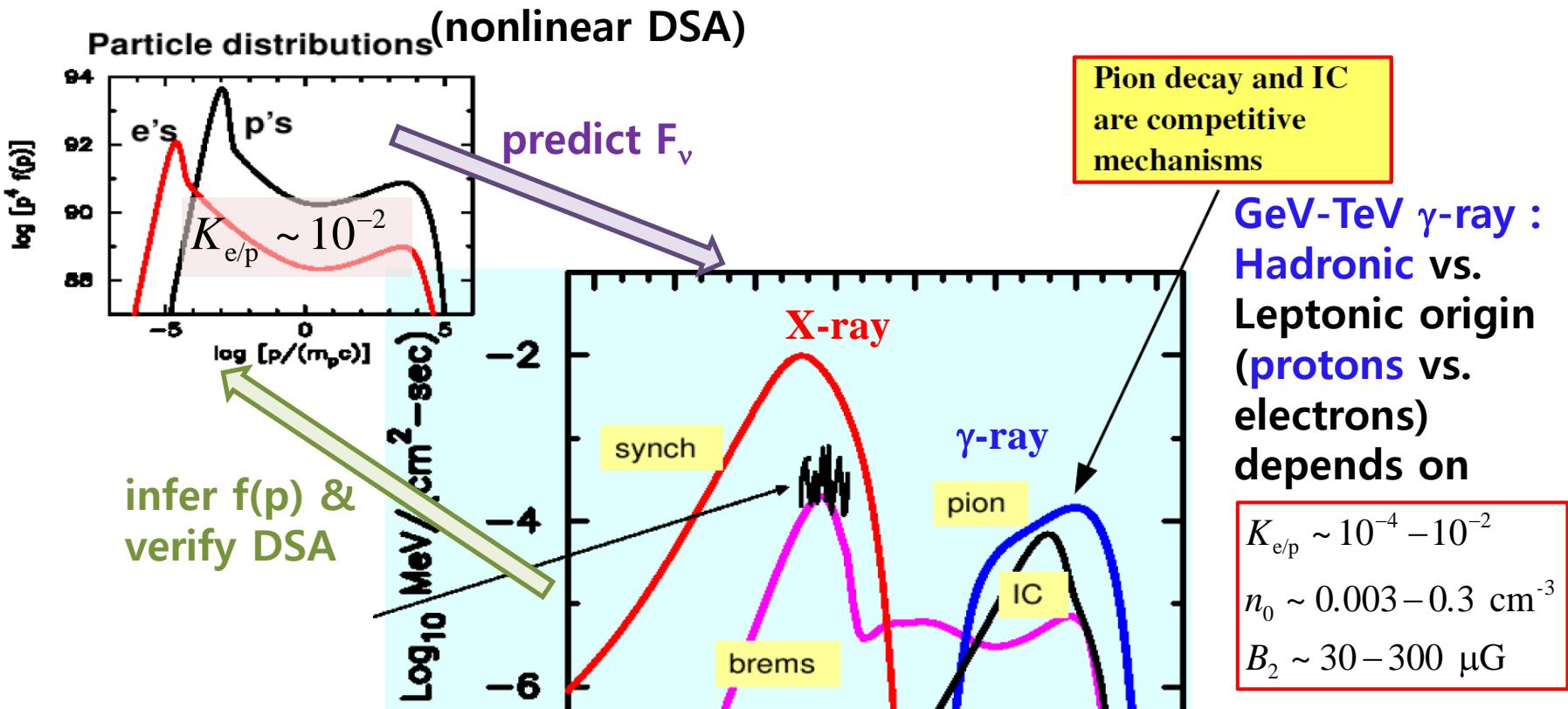
Pusan National University, Pusan, Korea

SNR = shock → CR acceleration → non-thermal radiation



Nonthermal radiation from CRs accelerated at SNR shocks

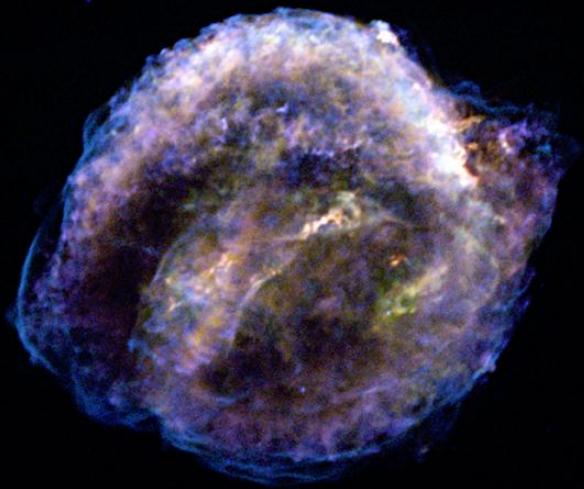
- CR e + B field \rightarrow Synchrotron (radio – X-ray)
- thermal & nonthermal bremsstrahlung
- CR p + p $\rightarrow \pi^0$ decay \rightarrow 100 GeV γ -ray
- CR e + CMBR \rightarrow Inverse Compton scattering \rightarrow TeV γ -ray



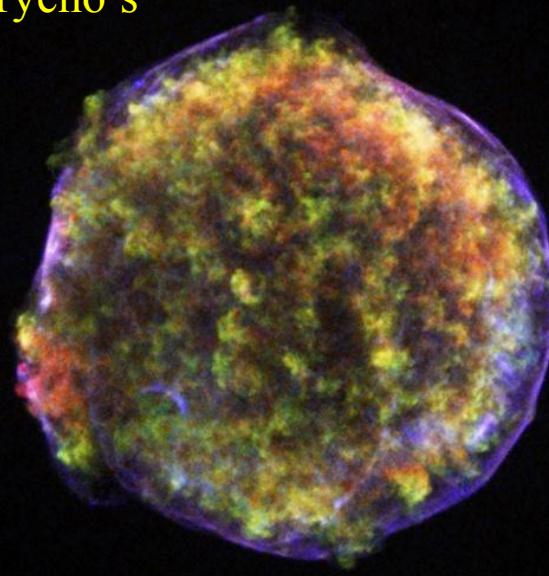
Provide observational evidence and constraints for CR acceleration.

X-ray observation → B field amplification

Kepler's



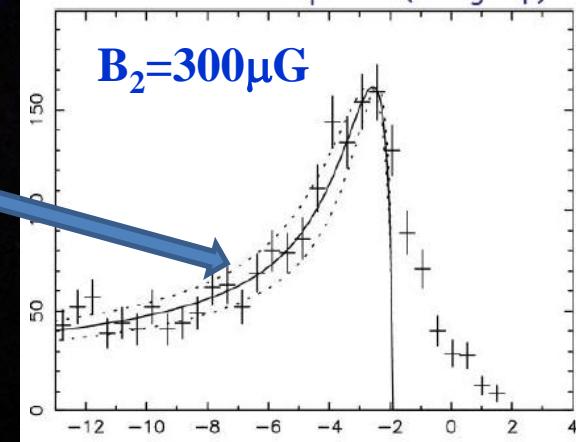
Tycho's



SN1006

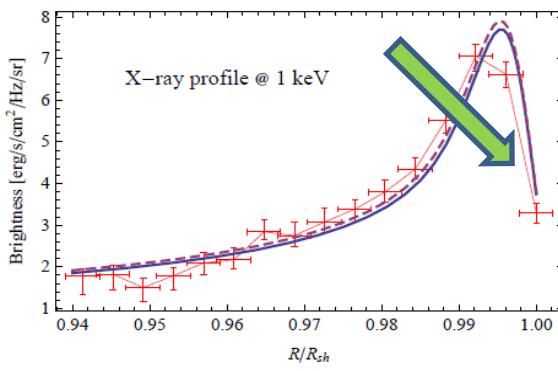
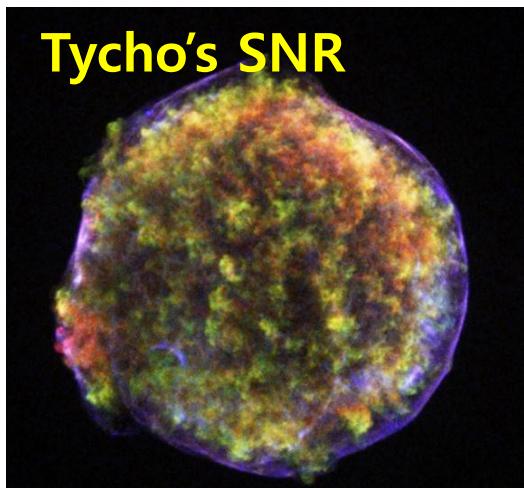


Chandra X-ray
Images of
SN Ia Remnants



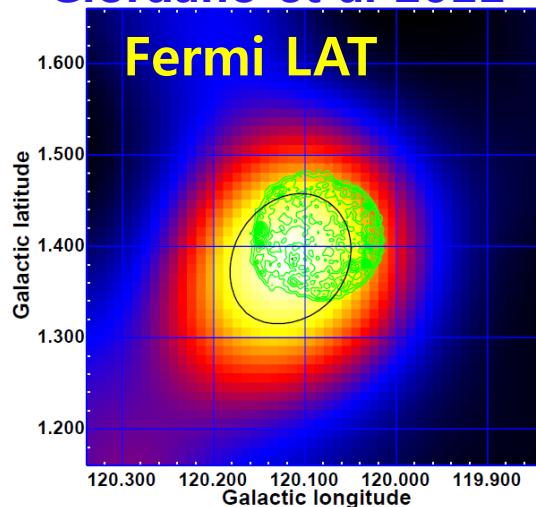
- thin filaments of nonthermal X-ray indicating fast synchrotron cooling
- $B_2 \sim \text{a few } 100 \mu\text{G}$ (**mag. field amplification**
Bell & Lucek 2000, Bell 2004)
- higher than ISM field of $\sim 5 \mu\text{G}$
- CR electrons with $E_{\text{ele}} \sim 10^{\text{'s TeV}}$

γ -ray emission from Tycho's SNRs \rightarrow steep proton spectrum



Projected X-ray emission
($B_2 = 300 \mu\text{G}$)
Chandra X-ray data at 1 keV.

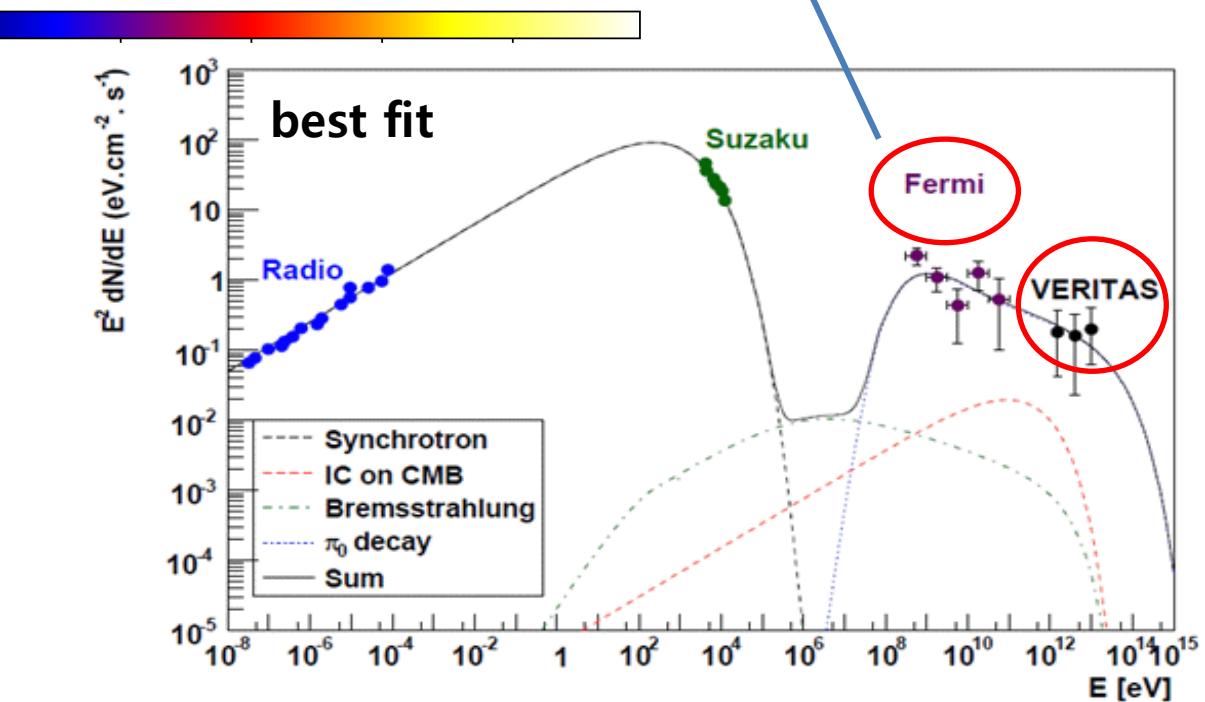
Giordano et al 2011

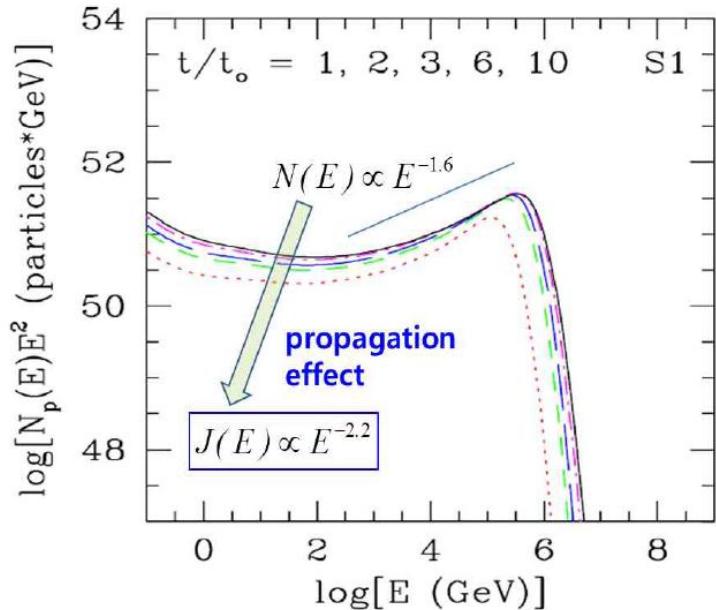
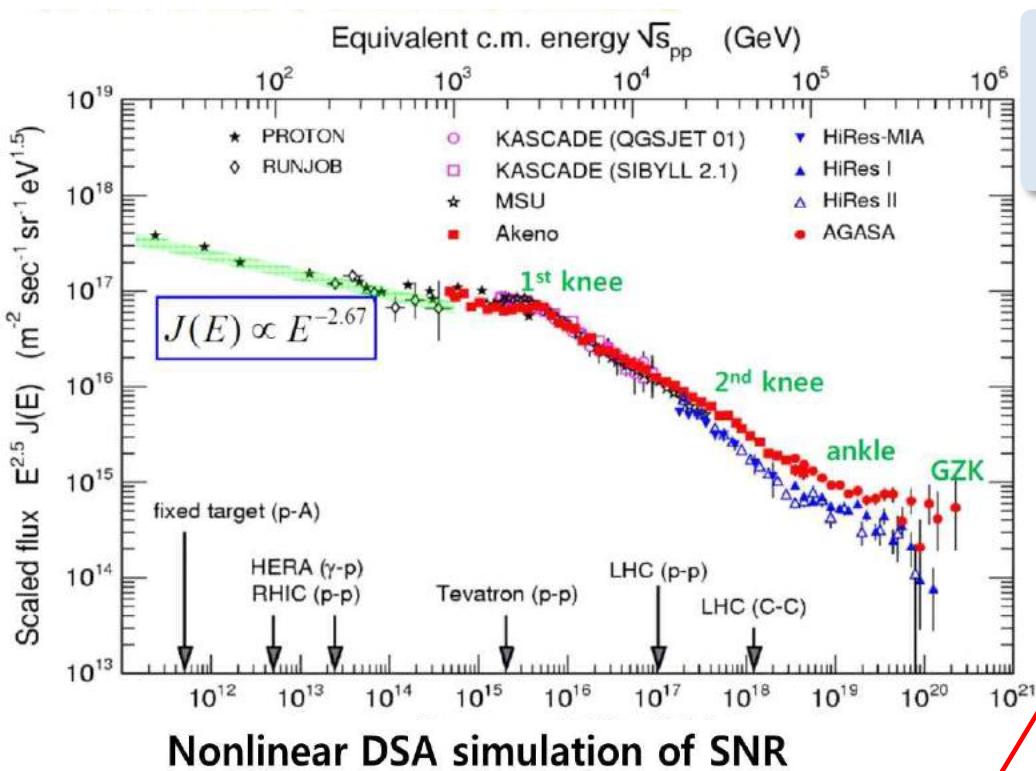


$$N_p(E) \propto E^{-2.3}$$

$$B_2 \sim 200 \mu\text{G}$$

Proton spectrum from γ -ray spectrum
steeper than test-particle power-law





**Observed CR spectrum at Earth:
J(E) → source spectrum N(E)**

$J(E) \propto E^{-2.7}$ below the knee
mean propagation length : $\Lambda \propto E^{-0.6}$
 $\Rightarrow N(E) \propto E^{-2.2}$ at source
(Ave et al. 2009)

- consistent with γ -ray observation
- steeper than the test-particle power-law

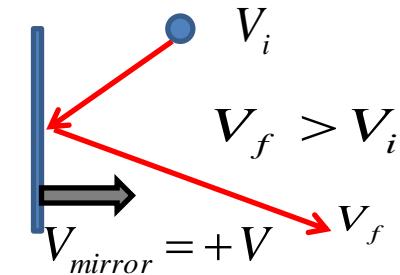
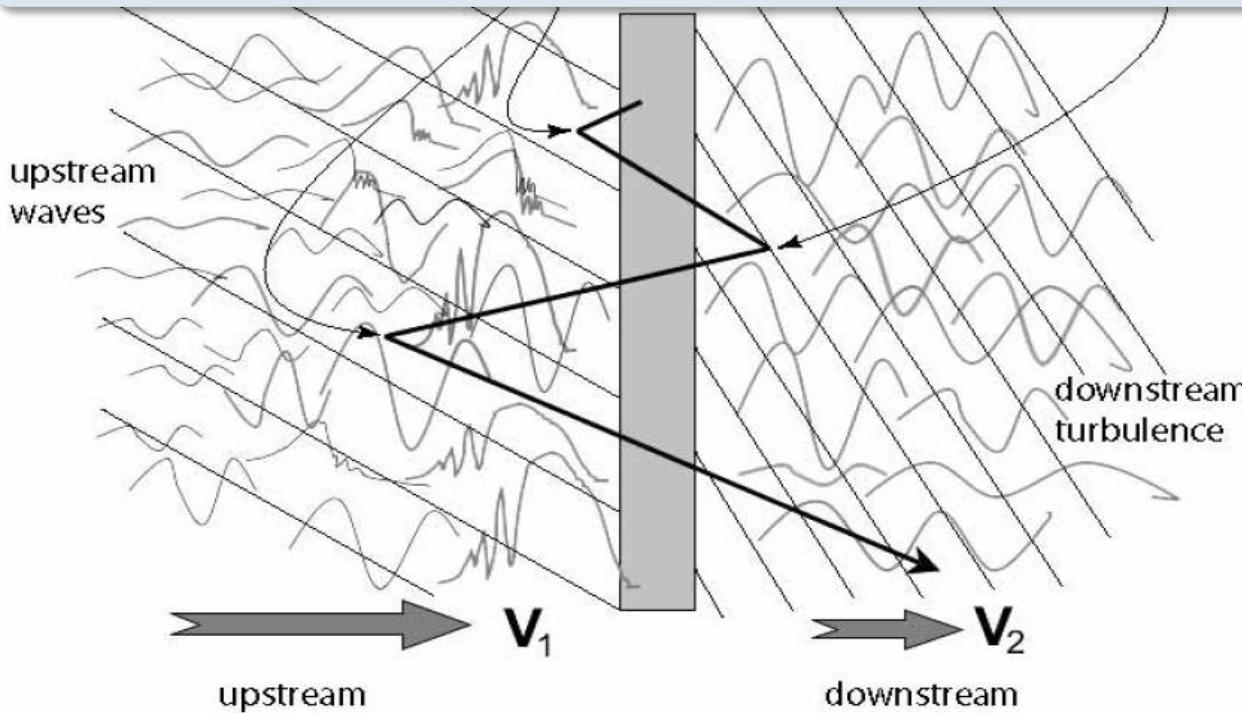
nonlinear DSA predicts :

$$N(E) \propto E^{-1.6}$$

Trouble with nonlinear DSA ??

Basics of Diffusive Shock Acceleration

Particle Acceleration at Shocks: Fermi 1st order



**Collision with approaching mirrors
→ gain energy**

Alfven waves in a converging flow act as converging mirrors

→ particles are scattered by waves and isotropized in local fluid frame

→ cross the shock many times, gain $\frac{\Delta p}{p} \sim \frac{u_1 - u_2}{v}$ at each shock crossing

Test-particle spectrum → non-thermal radiation spectrum

$f(p)$: isotropic part of momentum distribution function

$$f(p) \propto p^{-q} \text{ : power - law}$$

$$q = \frac{3V_2}{V_1 - V_2} = \frac{3r}{r-1}$$

r = compression ratio

for $M \gg 1$, $r = 4$, $q = 4$

$$N(E) \propto E^{-\gamma} \quad \gamma = q - 2 = 2$$



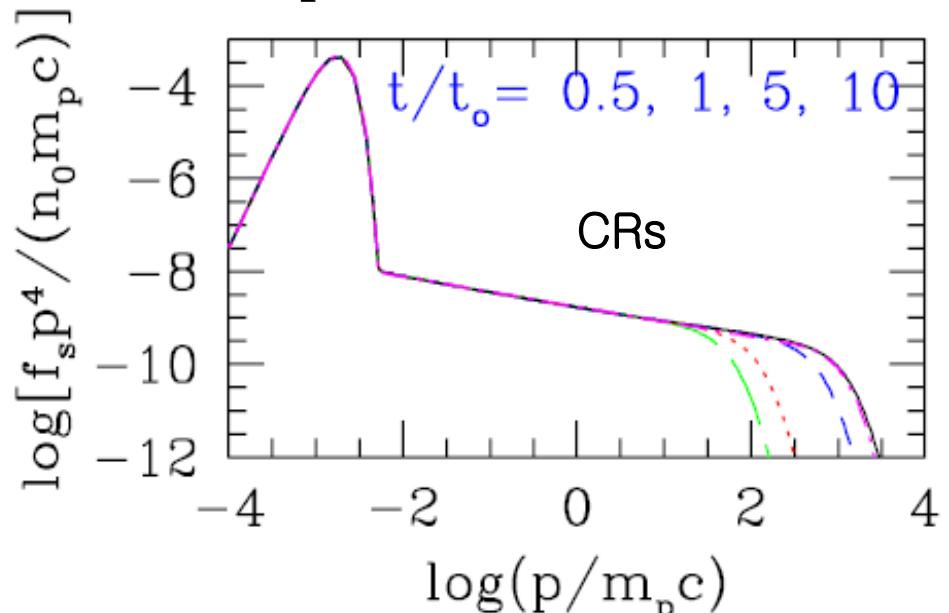
electron synchrotron + IC scattering photon spectrum at shock

$$j_v \propto v^{-\alpha}, \quad \alpha_{\text{syn(IC)}} = (q-3)/2, \quad \underline{\alpha_{\text{syn(IC)}} \approx 0.5 \text{ for } q=4}$$

proton + p collision $\Rightarrow \pi^0$ decay γ - ray spectrum

$$j_v \propto v^{-\alpha}, \quad \alpha_{\pi^0} \approx (q-2)/2, \quad \underline{\alpha_{\pi^0} \approx 1 \text{ for } q=4}$$

DSA kinetic simulation: $M_s=5$ shock thermal + power-law distribution

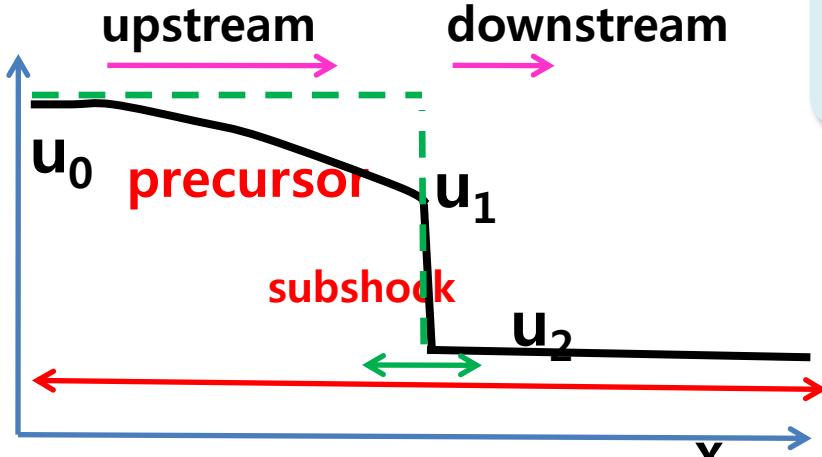


Test-particle vs. CR modified shock

when $P_{CR} \sim \rho u_s^2$

for $\kappa(p) = \kappa^* p^\alpha$

momentum dependent diffusion



$$l_{diff}(p_{min}) = \frac{\kappa(p_{min})}{u_s} \rightarrow u_1 - u_2$$

$$l_{diff}(p_{max}) = \frac{\kappa(p_{max})}{u_s} \rightarrow u_0 - u_2$$

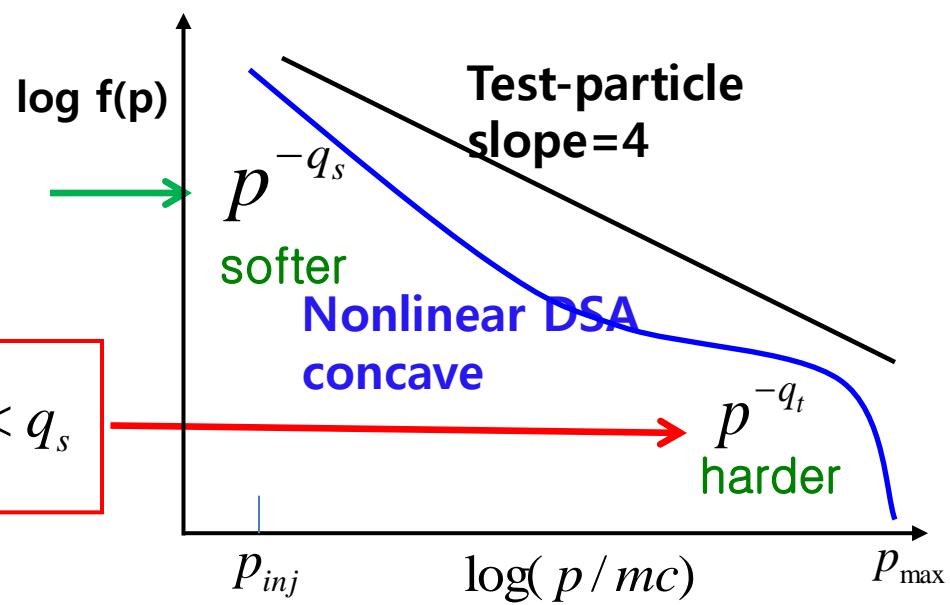
across the
subshock

$$q_s = \frac{3 \cdot (u_1)}{u_1 - u_2} > 4$$

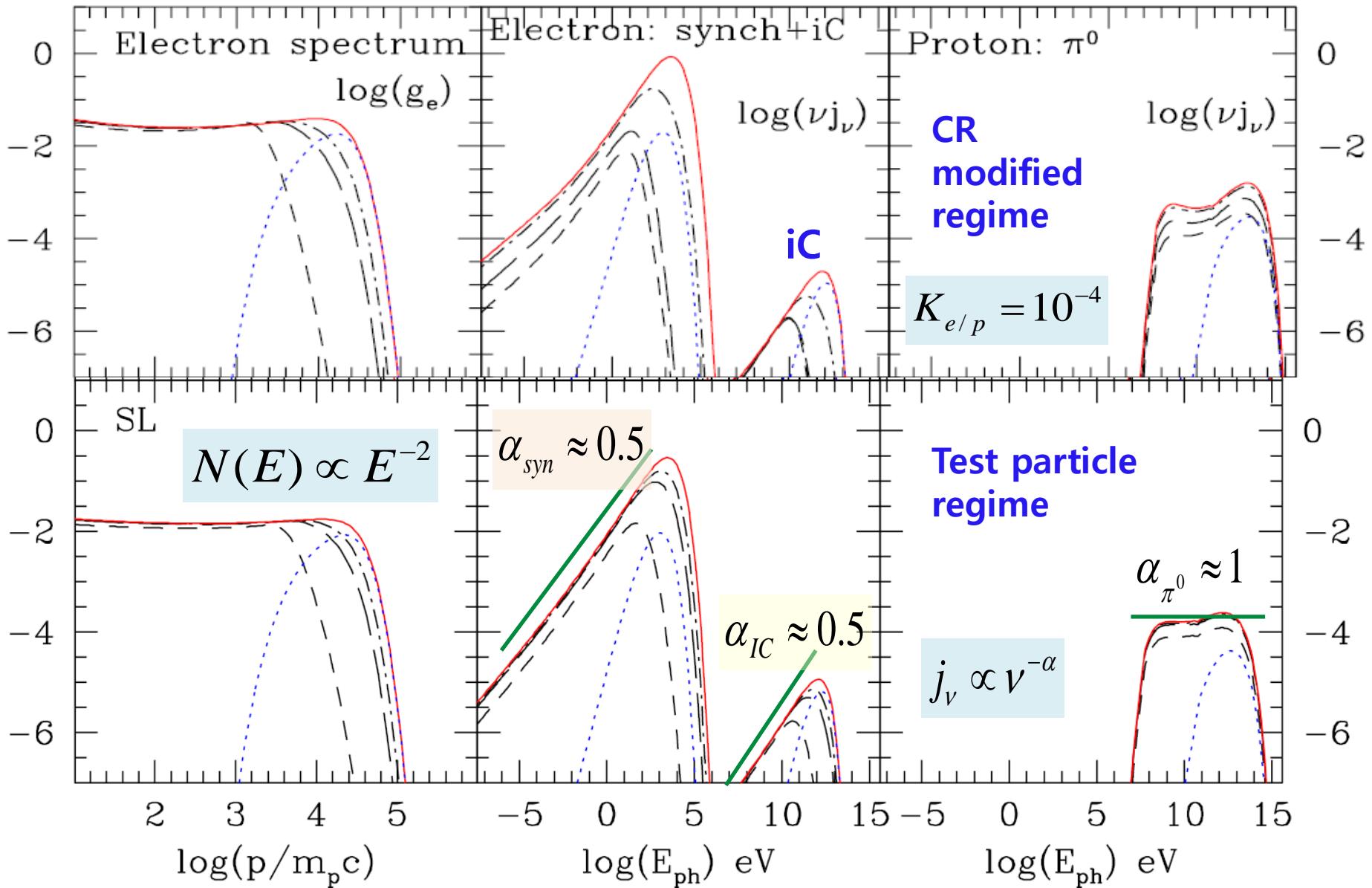
across the
total shock

$$q_t = \frac{3 \cdot (u_0)}{u_0 - u_2} < q_s$$

- shock precursor develops
- Particles with different p experience different Δu due to precursor



Nonthermal Radiation from SNR: DSA simulations Kang, Edmon, Jones 2012



at different locations: upstream, shock, & 3 downstream locations

B field amplification via plasma instabilities

streaming CRs upstream of shocks

→ excite resonant Alfvén waves

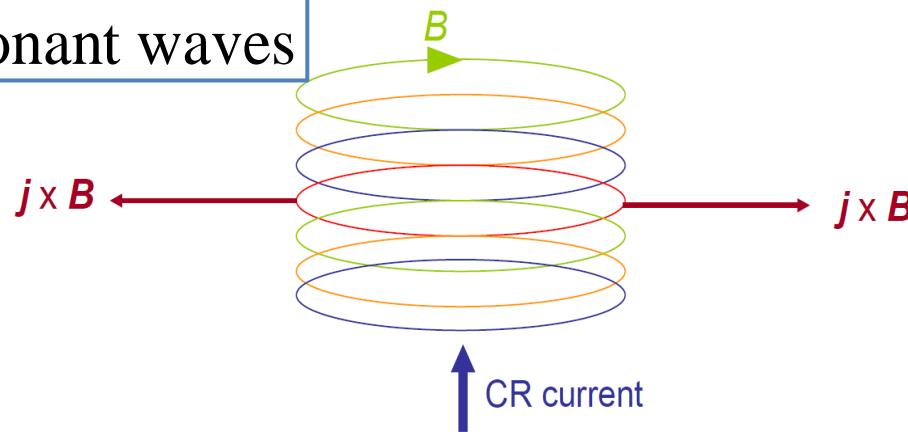
→ amplify B field (Bell 1978, Lucek & Bell 2000)

$$\lambda_w \sim r_g(p)$$

resonant waves

$$\lambda_w \ll r_g(p)$$

nonresonant waves



Streaming CRs

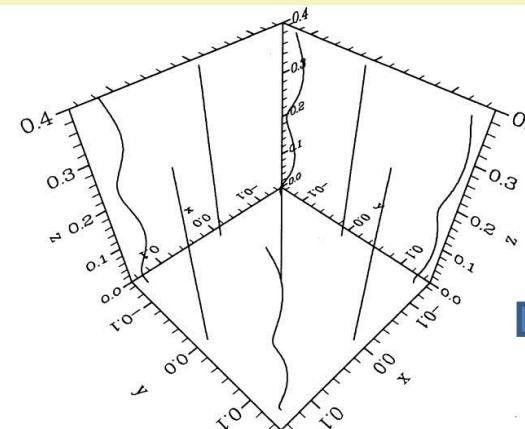


Figure 8. Magnetic field lines at $t = 0$ for the three-dimensional run.

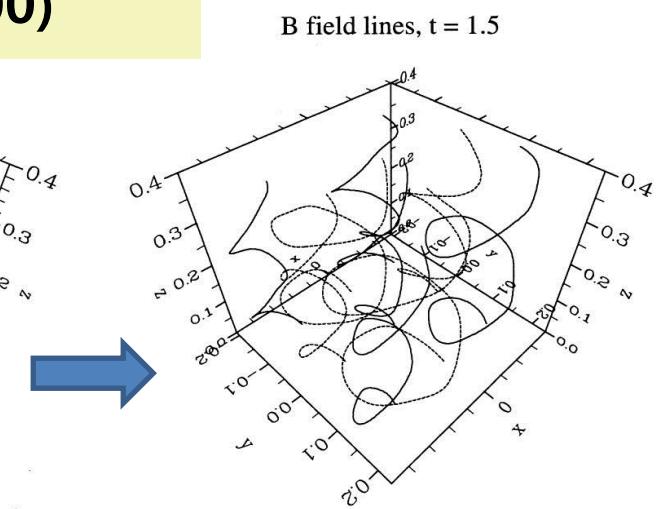
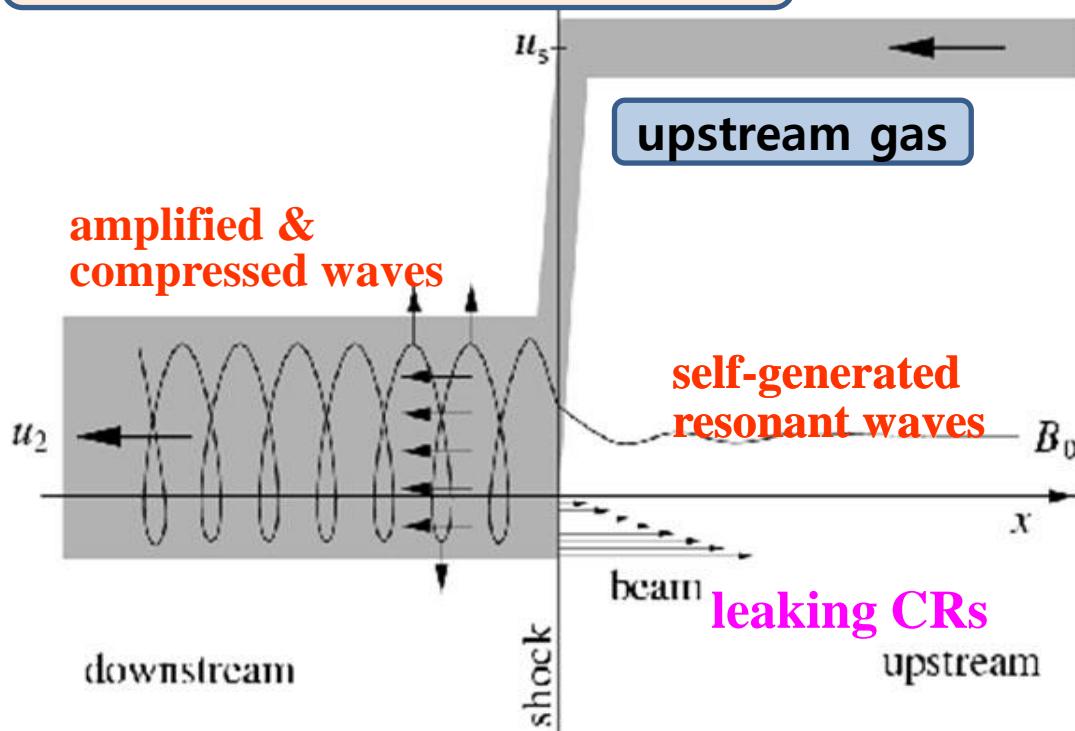


Figure 9. Magnetic field lines after 1.5 CR gyitations for the three-dimensional run.

Cosmic-ray current drives nonresonant instability by stretching field lines (Bell, 2004)

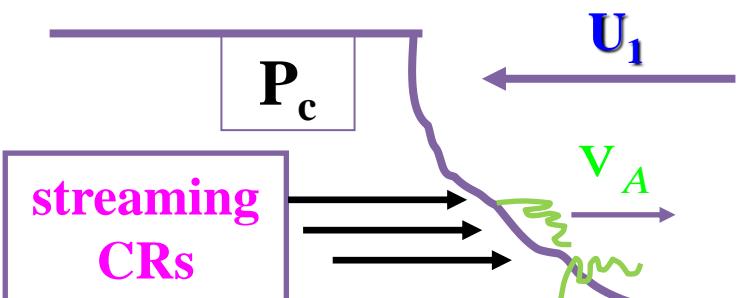
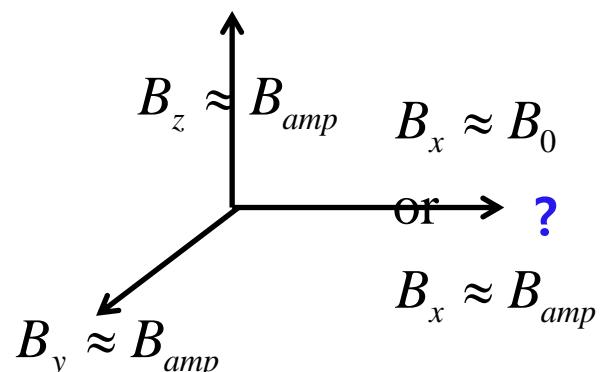
Wave excitation & drift



$$v_A = \frac{B_{\parallel}}{\sqrt{4\pi\rho}}$$

slow or fast drift ?

$$B_{\parallel} \approx B_0 \text{ or } B_{\parallel} \approx B_{amp}$$

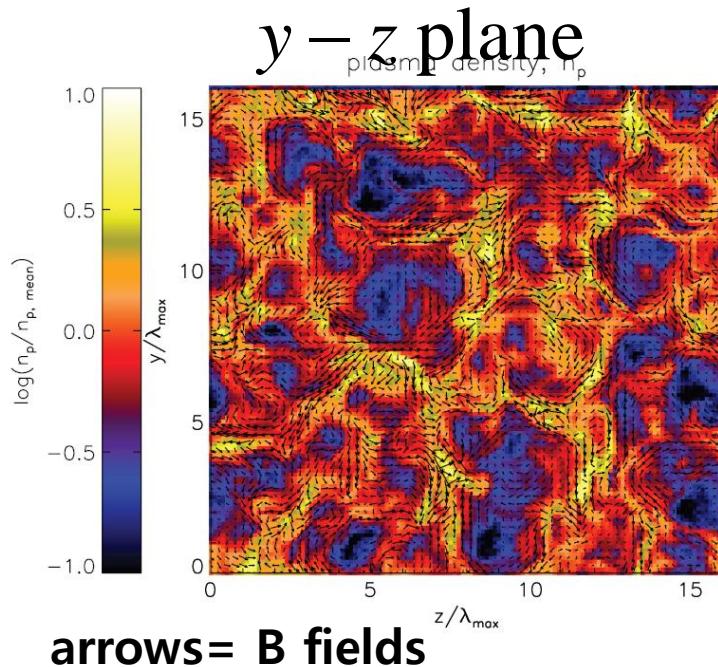


- waves are generated by streaming instability.
- waves drift upstream with $u_w \approx v_A$
- CRs are scattered and isotropized in the wave frame
- \rightarrow smaller $\Delta u \Rightarrow u - v_A$
- \rightarrow less efficient acceleration

Bell 1978

Bell's CR current driven instability

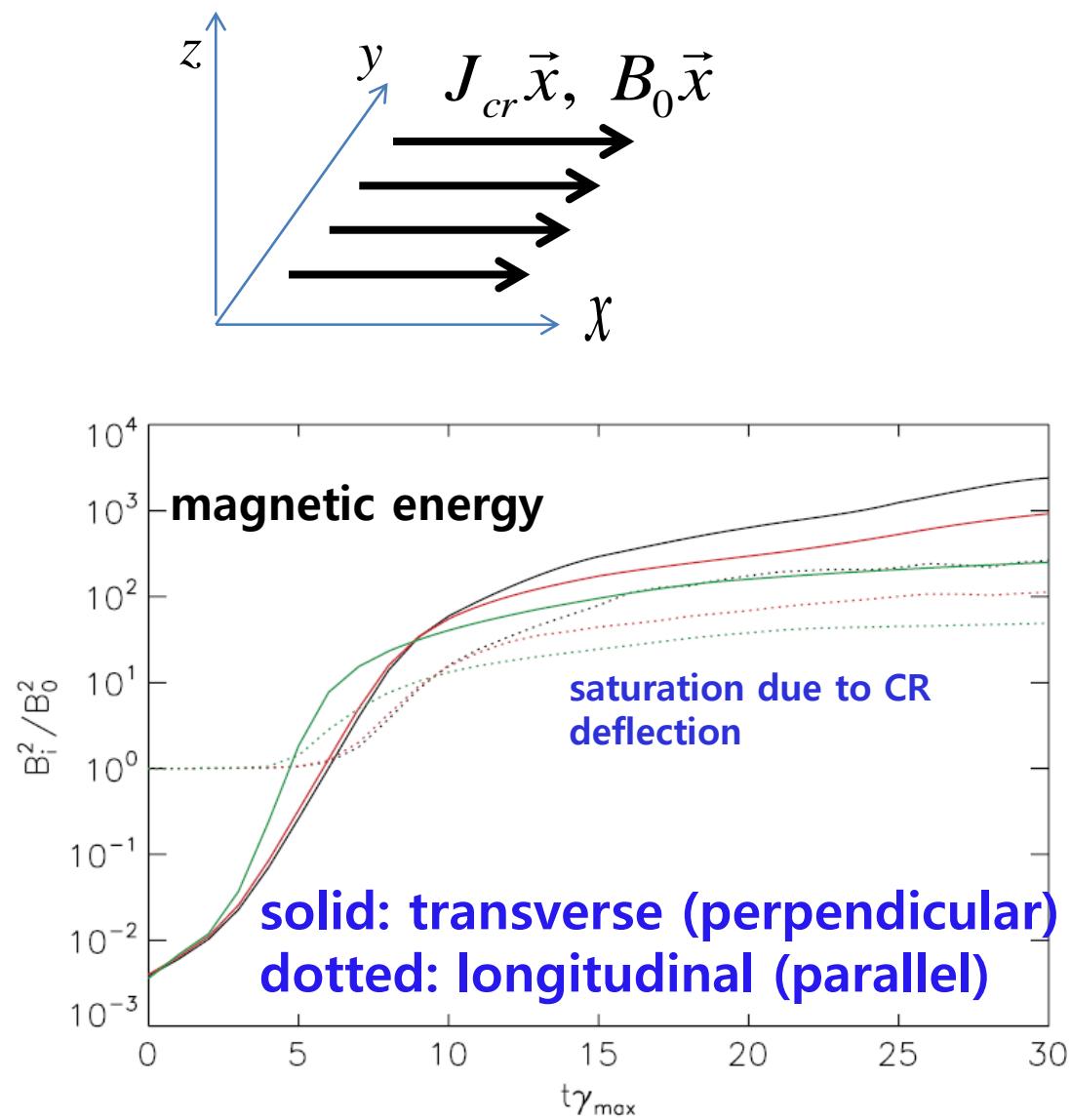
Riquelme & Spitkovsky 2009 PIC (Particle in Cell) simulation



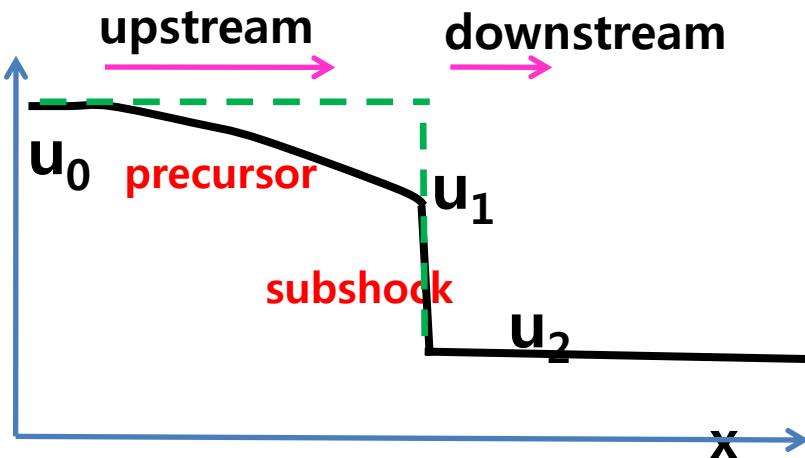
Confirmation of Bell's CR current driven instability

$$\rightarrow \frac{B_x}{B_0} \sim 10 \quad \frac{B_{y(z)}}{B_0} \sim 30$$

(parallel) (perpendicular)



CR modified shock structure



across the
subshock

$$q_s = \frac{3 \cdot (u_1 - v_A)}{u_1 - v_A - u_2}$$

across the
total shock

$$q_t = \frac{3 \cdot (u_0 - v_A)}{u_0 - v_A - u_2}$$

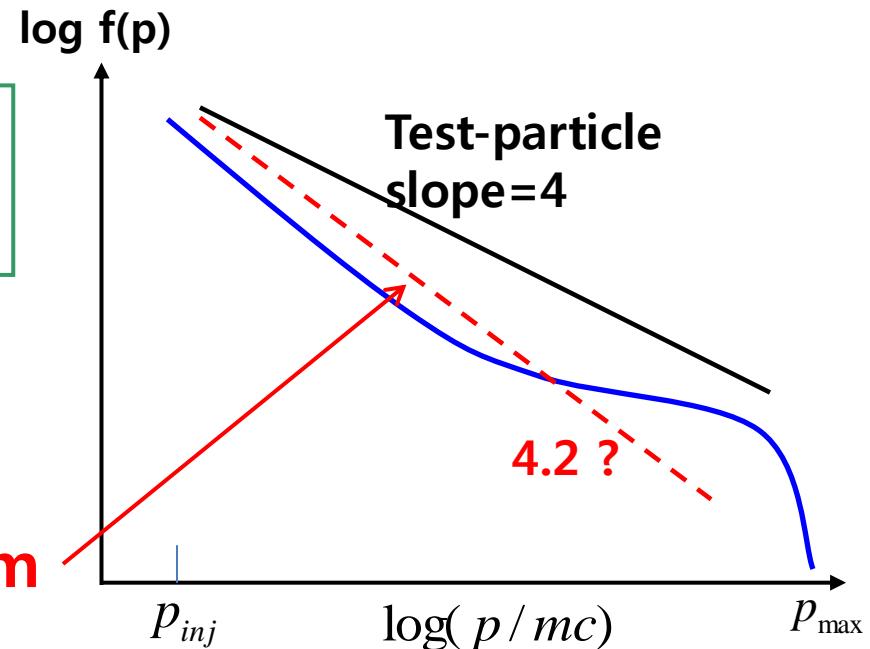
Alfvenic drift → softer spectrum

higher CR modification

⇒ larger B_1 & B_2 ⇒ larger v_A

⇒ steeper slope ⇒ less efficient acceleration

$$v_A = \frac{B_{\parallel}}{\sqrt{4\pi\rho}} \quad \text{Alfven speed}$$



**Highly nonlinear
problem !**

DSA kinetic simulations of SNRs

Basic Equations for DSA Simulations in diffusion approximation

$$\frac{\partial \rho}{\partial t} + \frac{\partial(\rho u)}{\partial r} = -\frac{2}{r} \rho u$$

(1D plane quasi-parallel shock)

$$\frac{\partial(\rho u)}{\partial t} + \frac{\partial}{\partial r}(\rho u^2 + P_g + \underline{P_c}) = -\frac{2}{r} \rho u^2 \quad \text{ordinary gasdynamics EQs + } P_c \text{ terms}$$

$$\frac{\partial(\rho e_g)}{\partial t} + \frac{\partial}{\partial r}(\rho e_g u + P_g u) = -u \frac{\partial P_c}{\partial r} - \frac{2}{r} (\rho e_g u + P_g u) + W - L$$

W = wave dissipation heating, L = thermal energy loss due to injection

Diffusion Convection Eq. with wave drift effect

$$\frac{\partial f}{\partial t} + (u + u_w) \frac{\partial f}{\partial r} = \frac{1}{3r^2} \frac{\partial}{\partial r} [r^2(u + u_w)] \cdot p \frac{\partial f}{\partial p} + \frac{1}{r^2} \frac{\partial}{\partial r} [r^2 \kappa(r, p) \frac{\partial f}{\partial r}] + Q(r, p)$$

$$\Rightarrow P_c = \frac{4}{3} \pi m_p c^2 \int_0^\infty f(p) \frac{p^4 dp}{\sqrt{p^2 + 1}} : \text{CR pressure}$$

$u_w \approx +v_A$ in upstream, $u_w \approx 0$ or $-v_A$ in downstream,

$\kappa(x, p) \approx \kappa^* p(\rho / \rho_0)^{-1}$: Bohm-like diffusion

$Q(x, p)$ = thermal leakage injection

Phenomenological models for wave-particle interactions

(See Caprioli 2012, Lee, Ellison, Nagataki 2012)

- **Alfven speed :** $V_A = \frac{B_0 + (B(r) - B_0)f_A}{\sqrt{4\pi\rho(r)}}$ with $f_A \sim 0.1 - 0.5$ parallel component of B field

- **B field amplification via plasma instabilities :**
depends on the modification (precursor) due to CR pressure

$$\frac{B(r)^2}{B_0^2} = 1 + (1 - \omega_H) \frac{4}{25} M_{A,0}^2 \frac{(1 - U(r)^{5/4})^2}{U(r)^{3/2}} \text{ in upstream } (r > R_s),$$

$$\frac{B_2}{B_1} = \sqrt{\frac{1}{3} + \frac{2}{3} \left(\frac{\rho_2}{\rho_1} \right)^2} \quad r = R_s; \quad B(r) = B_2 \cdot \frac{\rho(r)}{\rho_2} \text{ in downstream } (r < R_s),$$

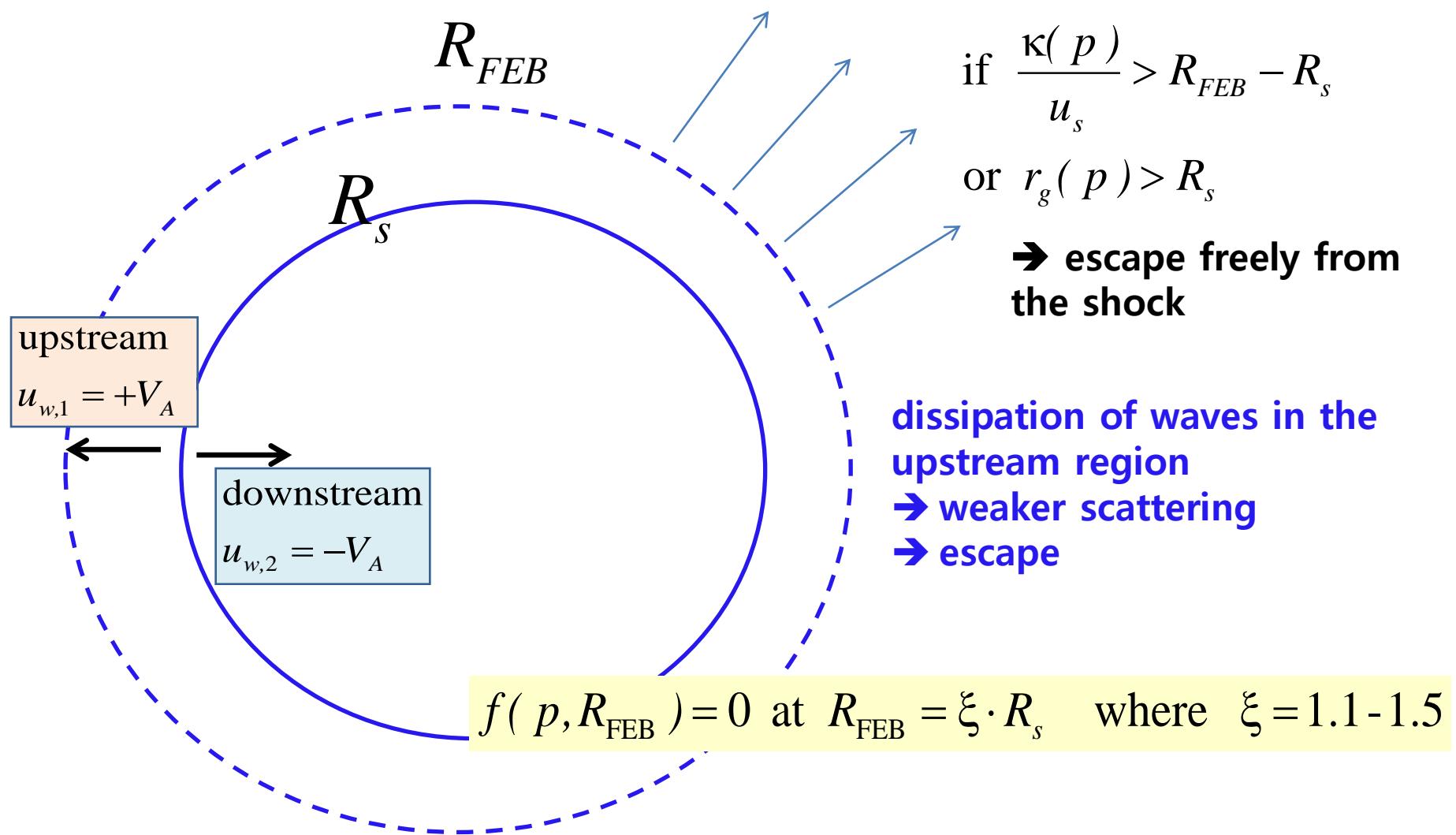
compression across the shock

$$\text{where } U(r) = [V_s - u(r)]/V_s, \quad M_{A,0} = V_s(t)/V_{A,0}, \quad V_{A,0} = B_0 / \sqrt{4\pi\rho_0}$$

- **Gas heating due to wave dissipation :** $W(r, t) = -\omega_H \cdot V_A(r) \frac{\partial P_c}{\partial r}$ with $\omega_H \sim 0.5$

- **Free Escape Boundary:** $f(p, R_{FEB}) = 0$ at $R_{FEB} = \xi \cdot R_s$ where $\xi = 1.1 - 1.5$

Escape of highest energy CRs from SNRs



SNR Model

$M_{ej} = 1.4 M_\odot$, $E_o = 10^{51}$ ergs
 $n_{ISM} = 0.3 \text{ cm}^{-3}$, $T_0 = 3 \times 10^4 \text{ K}$,
 $B_0 = 5 \mu\text{G}$
 $\Rightarrow M_s, M_A$

DSA model parameters

$\varepsilon_B = 0.23$: injection
 $f_A = 0.1 - 1.0$: V_A Alfvén speed
 $\omega_H = 0.5$: wave dissipation
 $R_{FEB} = (1.1 - 1.5) \cdot R_s$: FEB

upstream drift :

$$u_{w,1} = +V_A$$

downstream drift :

$$u_{w,2} = 0$$

Model parameters

Name ^b	n_H (cm $^{-3}$)	T_0 (K)	r_o (pc)	t_o (years)	f_A ^c	ω_H ^d	ζ ^e	$u_{w,2}$ ^f (km s $^{-1}$)	$v_{A,0}$
W1	0.3	3×10^4	3.18	255.	1.0	0.5	0.1	0	16.8
W2	0.3	3×10^4	3.18	255.	1.0	0.1	0.1	0	16.8
W3	0.3	3×10^4	3.18	255.	0.1	0.5	0.1	0	16.8
W4	0.3	3×10^4	3.18	255.	1.0	0.5	0.1	$-v_A$	16.8

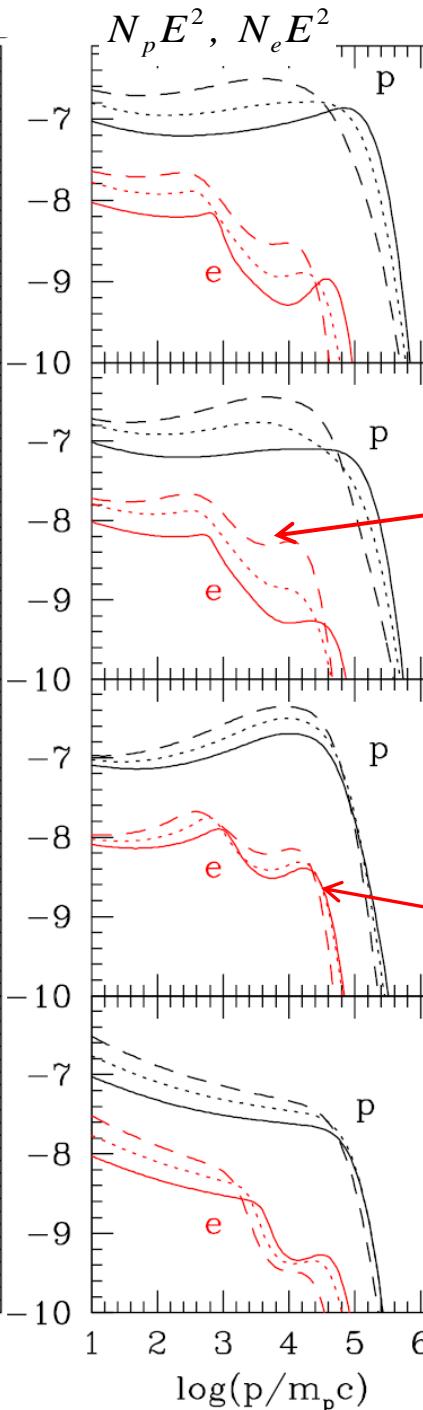
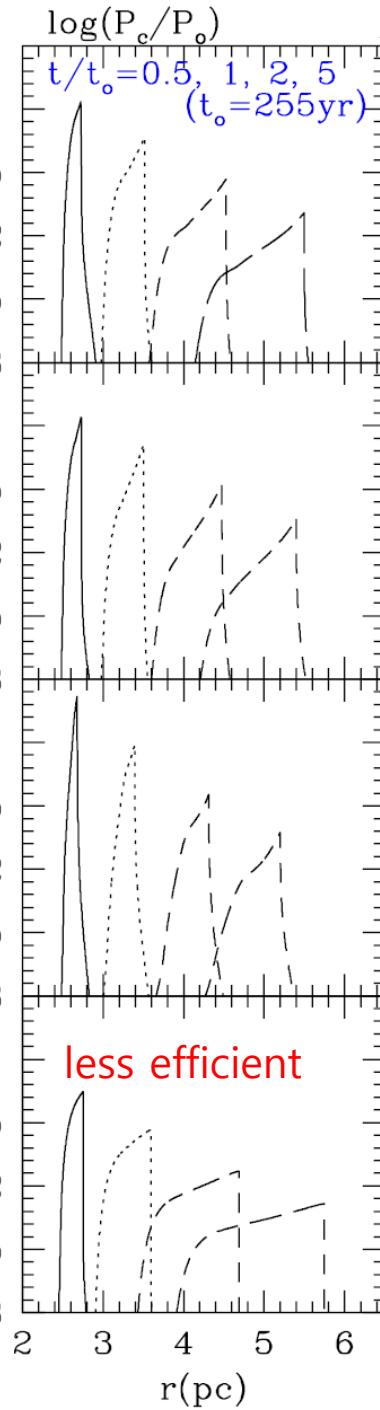
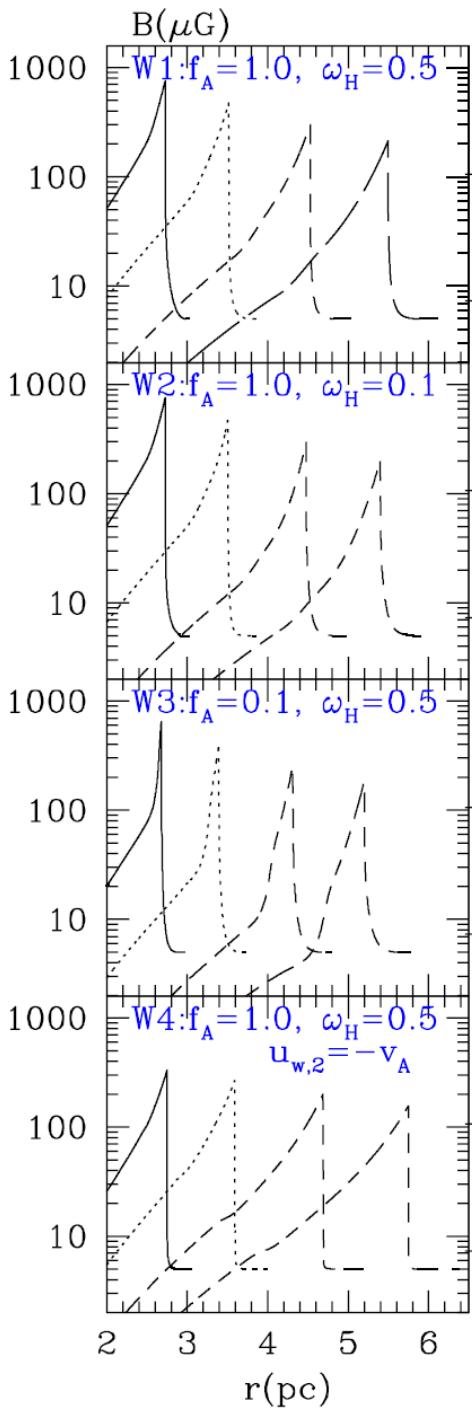
Strong shocks:

$$M_A \approx 180 \cdot \left(\frac{u_s}{3000 \text{ km/s}} \right), V_A = 16.8 \text{ km/s}$$

$$V_A = \frac{B_0 + (B(r) - B_0)f_A}{\sqrt{4\pi\rho(r)}}$$

$$M_s \approx 115 \cdot \left(\frac{u_s}{3000 \text{ km/s}} \right), c_s = 26 \text{ km/s}$$

$$\frac{B(r)^2}{B_0^2} \sim (1 - \omega_H) \frac{4}{25} M_{A,0}^2 \frac{(1 - U(r)^{5/4})^2}{U(r)^{3/2}}$$



- greater $B \rightarrow$
 higher $p_{p,max}$
 - history of $B(r,t)$ controls
 the shape of highest end
 of CR spectrum

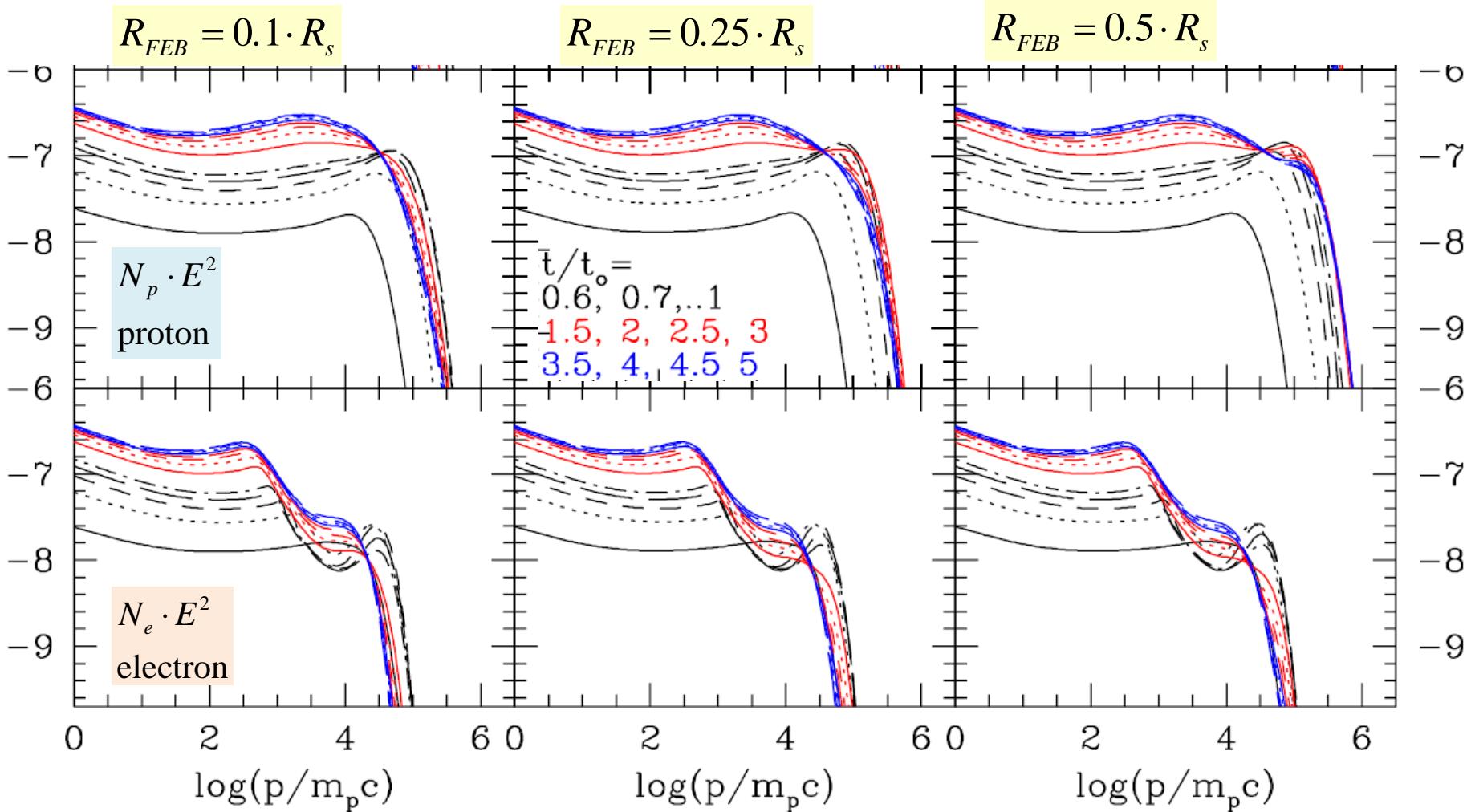
Electron cooling depends on the history of $B(r,t)$.

upstream component:
due to lower B_1

downstream drift:
 $u_{w,2} = -V_A$

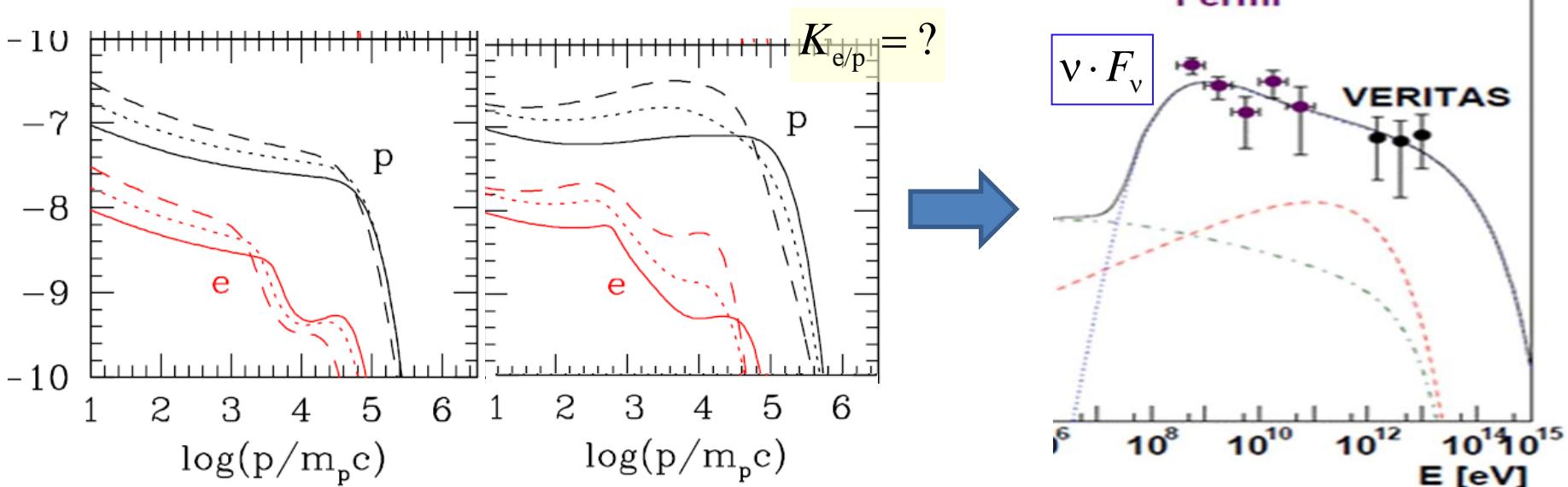
less efficient

Effects of Free Escape Boundary



- greater $R_{FEB} \rightarrow$ higher $p_{p,max}$
- R_{FEB} controls the shape of highest end of proton spectrum

Highest End of CR spectrum determines GeV-TeV γ -ray emission. So details of DSA modeling are important.



DSA model parameters

$\varepsilon_B = 0.2 - 0.23$: injection

$f_A = 0.1 - 1.0$: $V_A(r, t)$ Alfvén speed

$\omega_H = 0.5$: wave dissipation, MFA

$R_{FEB} = (1.1 - 1.5) R_s$: FEB

time - dependent evolution

$T_0 \Rightarrow M_s(t)$: sonic Mach no. \Rightarrow CR efficiency

n_0 & $B_0 \Rightarrow M_{A,0}$: Alfvén Mach no. \Rightarrow MFA, $B(r, t)$

$B(r, t) \Rightarrow V_A(r, t) \Rightarrow q$: power - law slope

$B(r, t) \Rightarrow p_{max,p}, p_{max,e}$ (cooling)

FEB & $B(r, t) \Rightarrow$ exponential tail

....

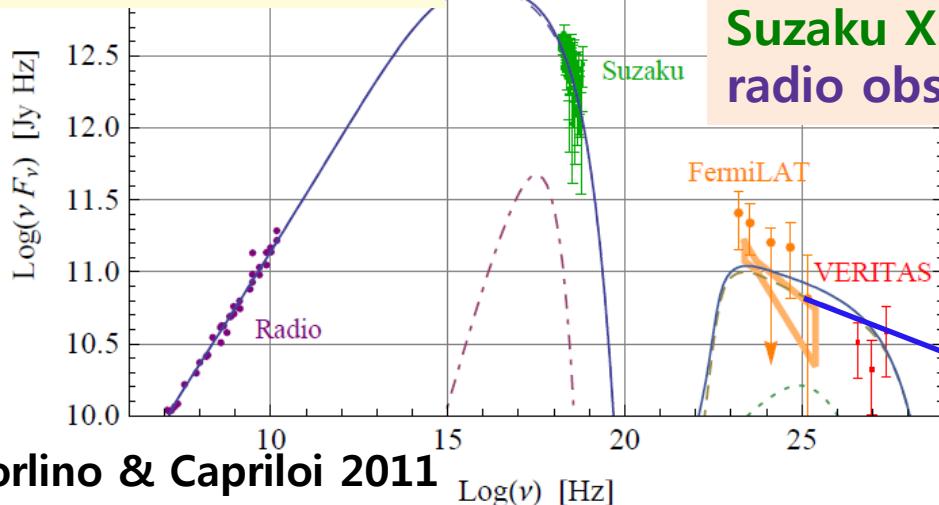
IV. Summary

- * Observations of Supernova Remnants
 - X-ray → amplified B fields: $B_2 \sim 100\text{-}300 \mu\text{G}$
 - γ -ray → hadronic π^0 emission confirmed
 - proton spectrum: $N_p(E) \propto E^{-2.2} - E^{-2.3}$ required
- * Hybrid/PIC plasma simulations have shown that
 - streaming and current driven instabilities → amplify B
 $\delta B / B_o \sim 10 - 30$ is possible
- * Wave drift may cause steepening of CR spectrum
 - Nonlinear DSA can be consistent with γ -ray observation
 - Detail modeling of DSA & time-dependent history are important in predicting non-thermal radiation spectrum

Nonthermal emission from nonlinear DSA vs. multiband observations

Observed Spectrum

Tycho SNR:



Morlino & Caprioli 2011

**VERITAS(TeV),
Fermi-LAT (GeV),
Suzaku X-ray,
radio observation**

$$n_0 = 0.3 \text{ cm}^{-3}$$

$$T_0 = 10^4 \text{ K}$$

$$R_s = 3.94 \text{ pc}$$

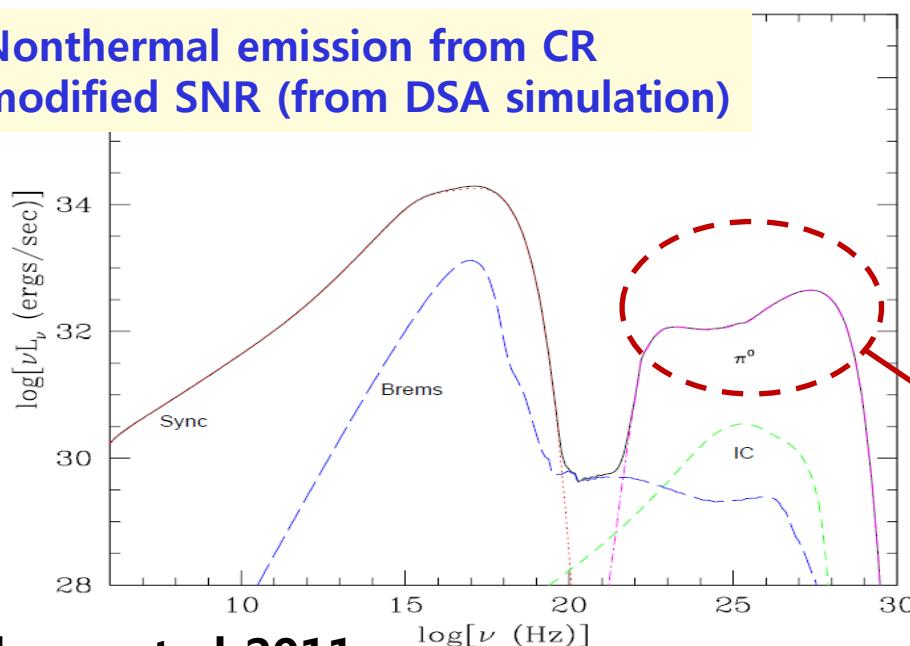
$$V_s = 5000 \text{ km/s}$$

$$B_2 = 300 \mu\text{G}$$

proton spectrum

$$N(E) \propto E^{-2.2} - E^{-2.3}$$

Nonthermal emission from CR modified SNR (from DSA simulation)



Edmon et al 2011

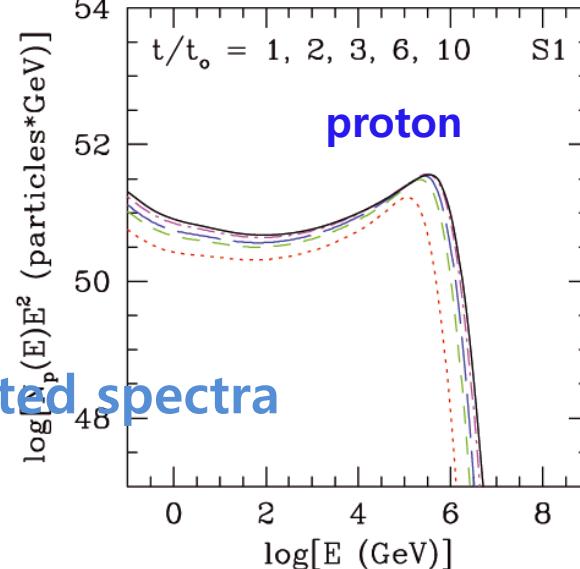
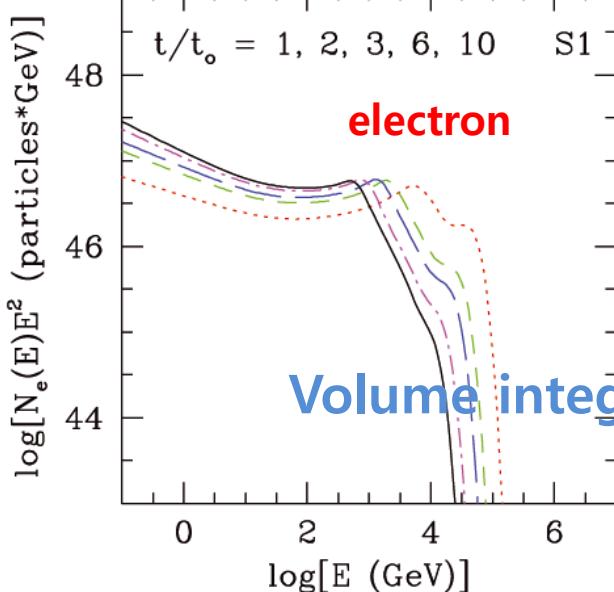
**synchrotron (dotted line),
IC (short dashed line)**

**bremsstrahlung (long dashed line),
π⁰ decays (dot-dashed line)**

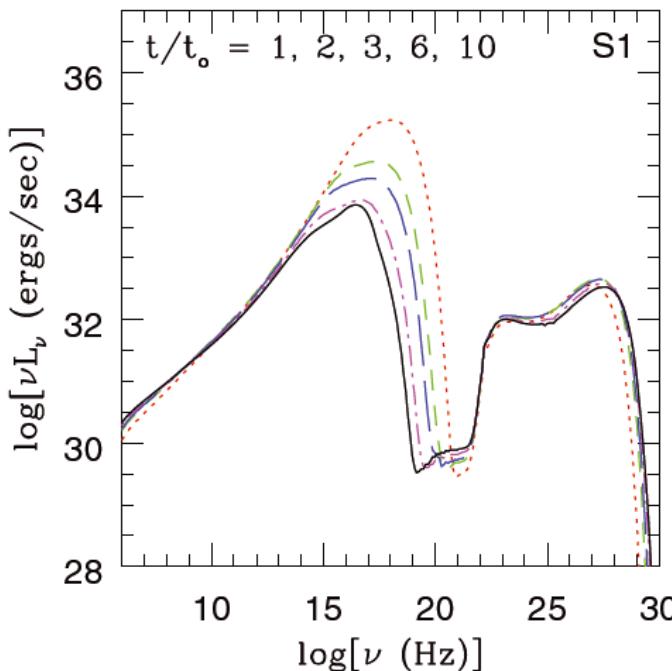
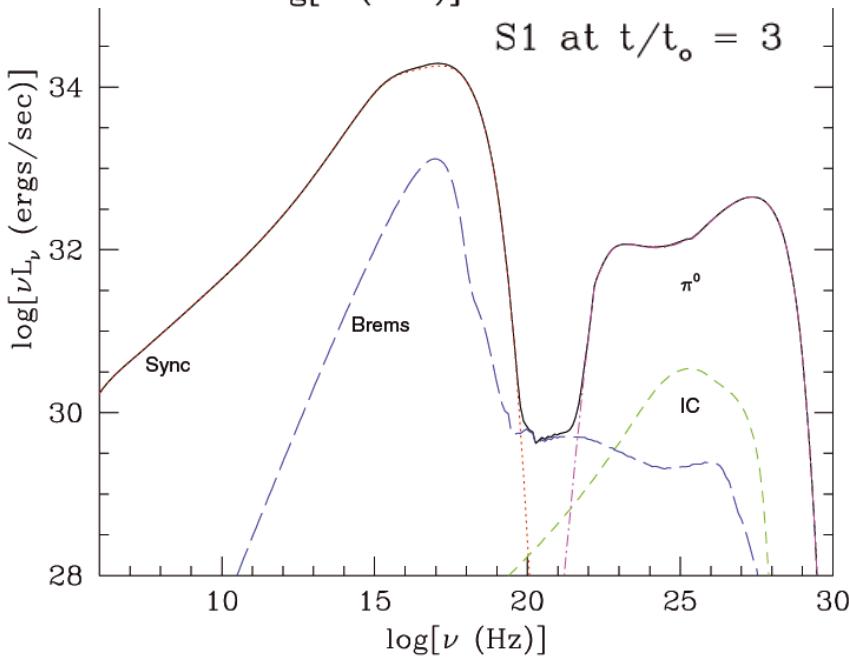
Nonlinear DSA: too efficient ?

- wave drift
 - escape of highest energy CRs
 - damping of turbulent waves
- Steepening of spectrum

Nonlinear DSA simulations of Type Ia SNR: Edmon, Kang, Jones, Ma 2011



$n_0 = 0.3 \text{ cm}^{-3}$
 $T_0 = 3 \times 10^4 \text{ K}$
 $B_0 = 30 \mu\text{G}$
 $B_2 \cong 210 \mu\text{G}$
 $t_o = 255 \text{ yrs}$
 $K_{e/p} = 10^{-4}$



CR ion injection

Gargate & Spitkovsky 2011
Hybrid simulation in 2D

$M_A=3.1$, parallel shock

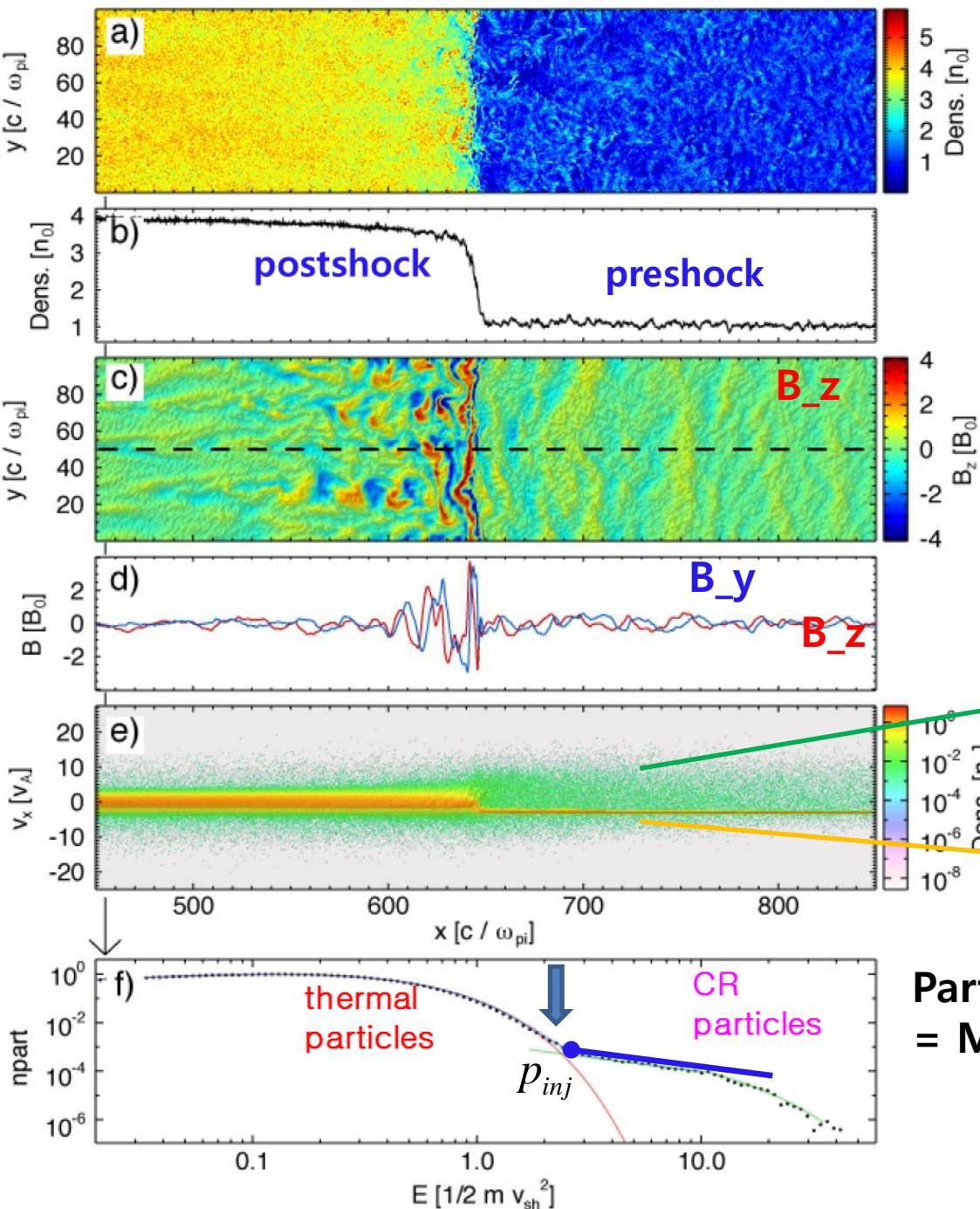
Self-generated
resonant waves

Two stream instabilities

Protons streaming upstream

Incoming cold beam

Particle spectrum
= Maxwellian + power-law tail



DSAed CR spectrum vs. photon spectrum

CR spectrum in test - particle regime

$$f_{DSA}(p) \propto p^{-q}, \quad N(E) \propto E^{-(q-2)},$$

→ electron synchrotron + IC scattering photon spectrum at shock

$$j_\nu \propto \nu^{-\alpha}, \quad \alpha_{\text{syn(IC),shock}} = (q-3)/2, \quad \alpha_{\text{syn(IC),shock}} \approx 0.5 \text{ for } q=4$$

volume integrated spectrum of electrons steepens by +1 in slope

$$F_e(p) = \int f_e(p, x) dx \propto p^{-q-1} \text{ (due to cooling) above } p_{break}(t)$$

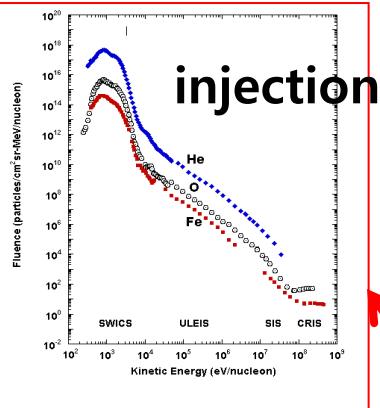
→ integrated photon spectrum (unresolved observation)

$$J_\nu \propto \nu^{-\alpha}, \quad \alpha_{\text{syn(IC),integ}} = \alpha_{\text{syn(IC),shock}} + 0.5, \quad \alpha_{\text{integ}} \approx 1.0 \text{ for } q=4 \quad \text{X-ray}$$

volume integrated spectrum of proton spectrum

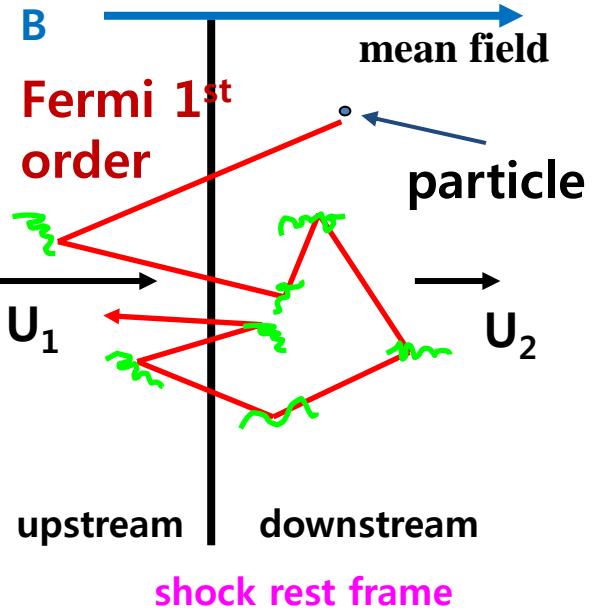
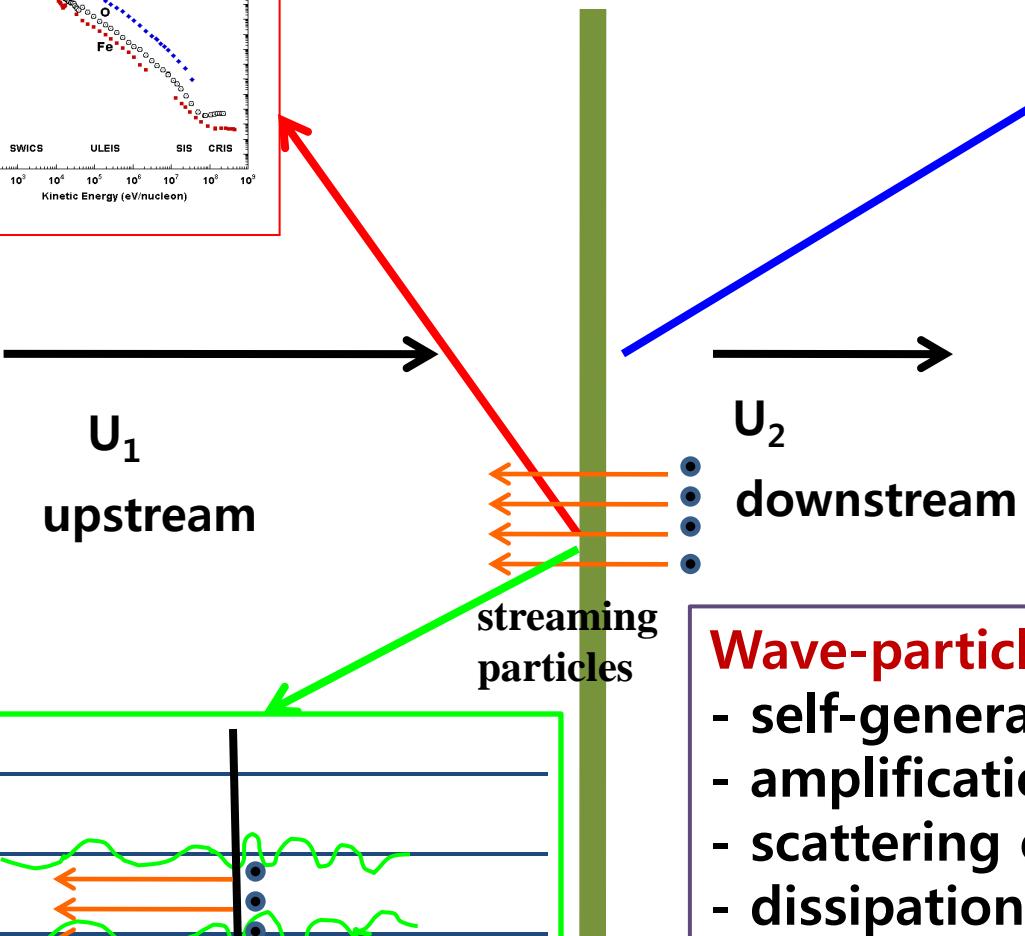
proton + p collision $\Rightarrow \pi^0$ decay γ - ray spectrum

→ $J_\nu \propto \nu^{-\alpha}, \quad \alpha_{\pi^0} \approx (q-2)/2, \quad \alpha_{\text{shock}} \approx 1 \text{ for } q=4 \quad \text{GeV-TeV}$



Key Physics of DSA

Shock front



Wave-particle interactions important

- self-generated waves (res. & non-res)
- amplification of B fields
- scattering of particles (diffusion)
- dissipation of waves
- ion injection
- electron heating & injection