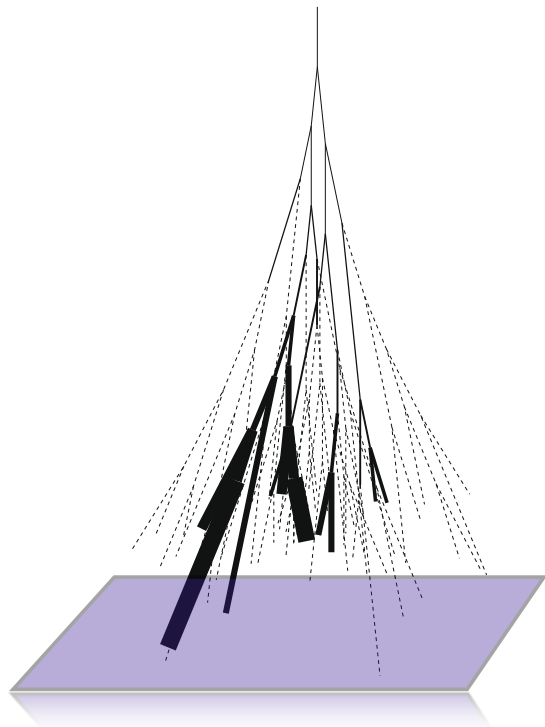


Attaching weight

De-thinning method (P. Billion, AUGER group)



2010.09.10

Soonyoung Roh

Chungnam National University

Korea Numerical Astrophysics Group (KNAG)

Introduction

What are **Ultra High Energy Cosmic Rays (UHECRs)**?

Cosmic rays elementary particles, nuclei, and electromagnetic radiation of extra-terrestrial origin.

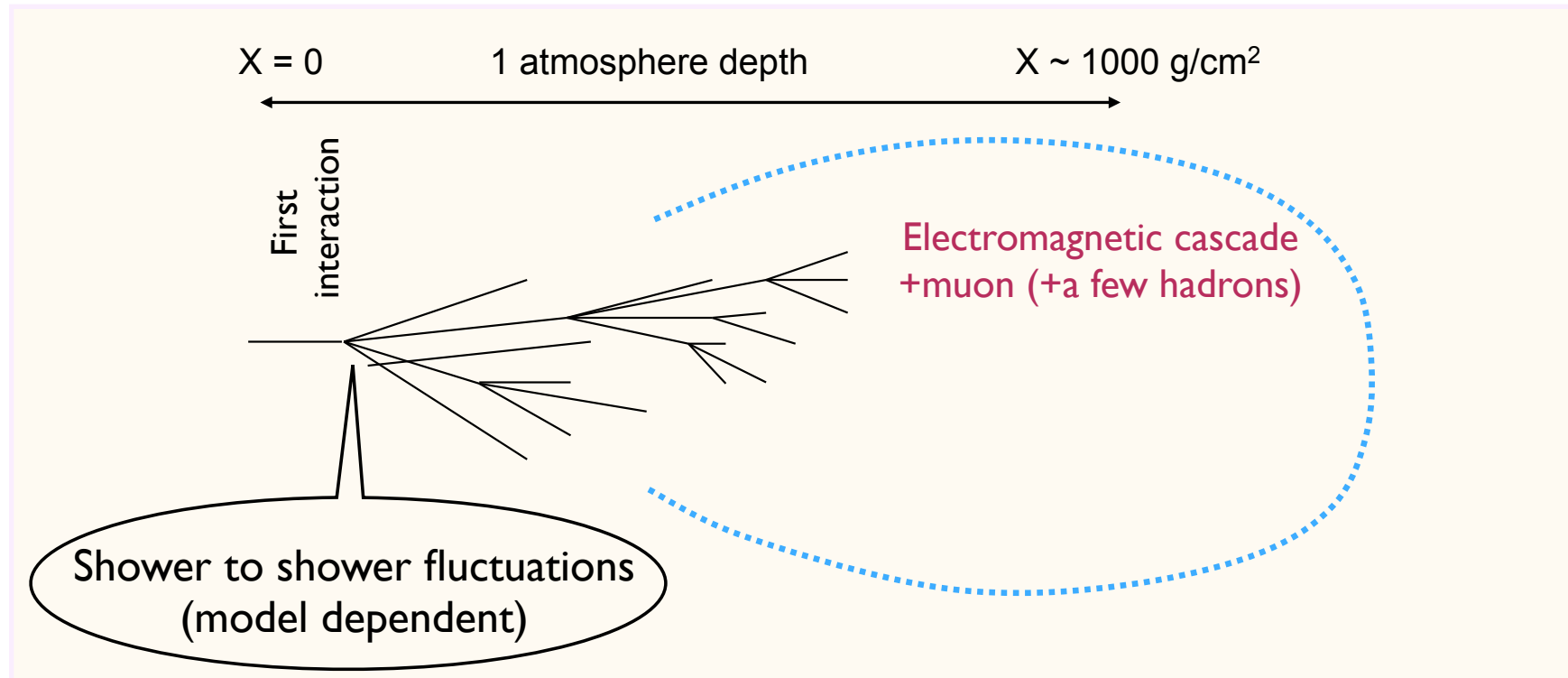
Ultra-high energy cosmic rays?

- **cosmic rays with energies above $\sim 10^{18}$ eV**

The Mystery of Ultra-High Energy Cosmic Rays

- How are **UHECRs** accelerated to such extreme energies?
- Where do **UHECRs** come from?
- What is the composition of the **UHECRs**?

Particles generate from air shower simulation



How to simulate an EAS ?

Follow the particles and their fate

Main effect of initial fluctuations :
Global translation of em. Cascade
Modulation of muon rate

Air shower simulation

COSMOS : Hybrid with sub-shower library (Kasher et al)

MOCCA : Split algorithm, thinning, Pascal (Hillas)

AIRES : transcript of MOCCA to Fortran (Scout)

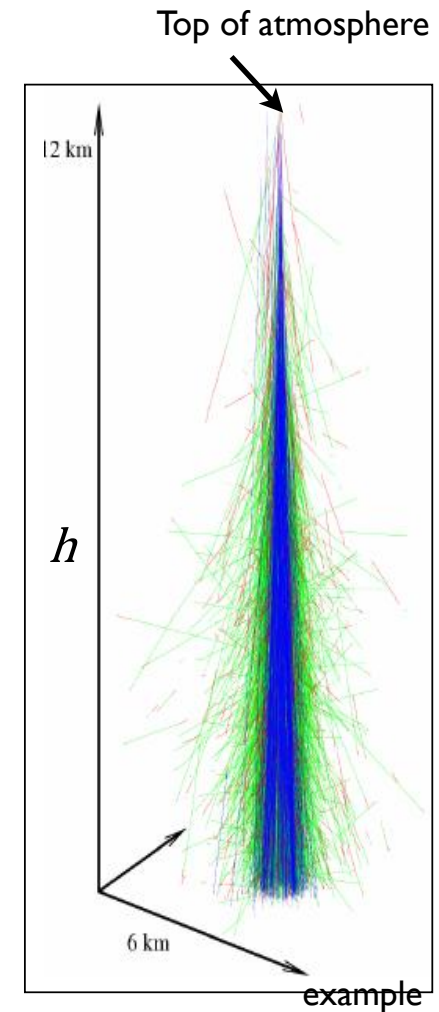
SENECA : Hybrid with cascade equations (Drescher et al)

...

Probabilities (transport, interactions):

Decision by random numbers

→ Monte Carlo method



Particle for Interaction

The probability P_{int} to traverse a layer with thickness χ **without interaction** is

$$P_{\text{int}}(\chi) = \frac{1}{\lambda_{\text{int}}} e^{-\chi/\lambda_{\text{int}}}$$

The individually traversed matter thickness χ is $\chi = -\ln(\text{RNDM}) \cdot \lambda_{\text{int}}$
with random number $0 < \text{RNDM} < 1$

The mean free path λ_{int} is given by $\lambda_{\text{int}} = \frac{\sum_{i=1}^n n_i A_i}{\sum_{i=1}^n n_i \sigma_{i\text{int}}}$

with A_i = atomic weight of component i

and σ_{int} = (energy dependent) cross-section of component i

The **atomic fractions n_i** (volume) of air are adopted to

N₂	0.7848	(78.084%)
O₂	0.2105	(20.948%)
Ar	0.0047	(0.934%)

Seed: every integer number l with $1 \leq l \leq 900\,000\,000$ starts an independent random number sequence

Particle for Decay

The probability P_D to traverse a path l **without decay** is

$$P_D(l) = \frac{1}{l_D} e^{-l/l_D}$$

The individually traversed path length l is $l = -\ln(\text{RNDM}) \cdot l_D$
with random number $0 < \text{RNDM} < 1$

The mean free path l_D is given by $l_D = c \cdot \tau \cdot \gamma \cdot \beta$

with

- c = vacuum speed of light,
- τ = particle life time at rest,
- γ = particle Lorentz factor and
- β = particle velocity in units of c

Thinning method vs. Full M.C (no-thinning)

What is the problem from no-thinning?

-Not enough disk space, Save CPU time

Why we need a thinning in the air shower simulations?

-we can't be tracked the created particles, only selected ones

How can we solve from this problem?

-Random sampling from particle energy

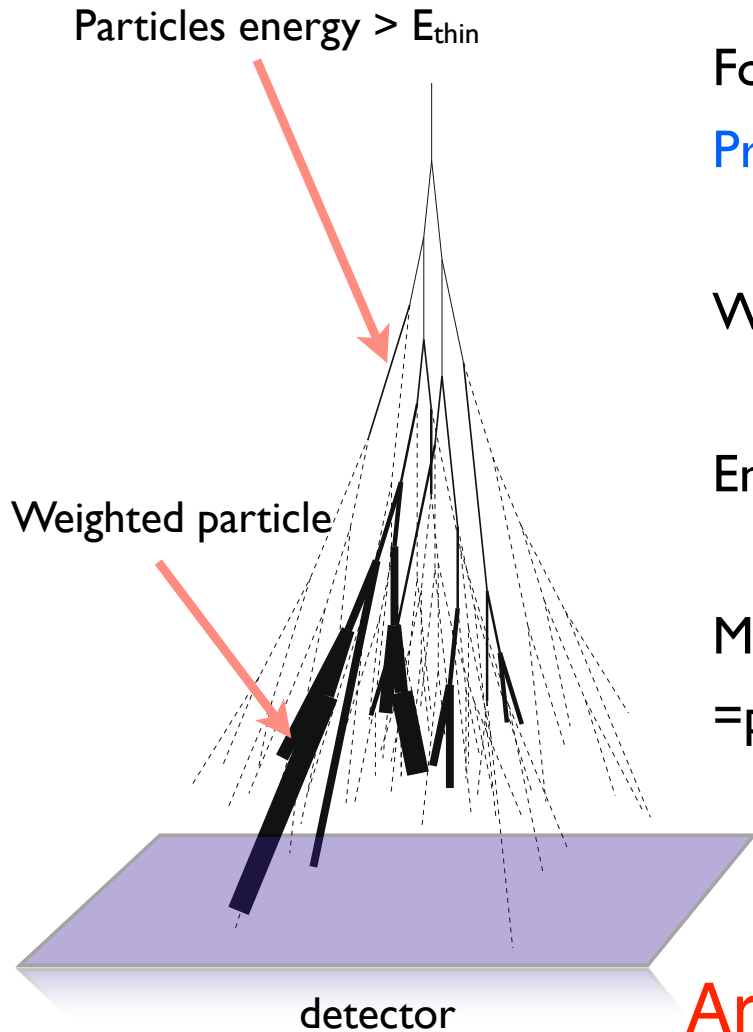
weight to selected particles

Goal

De-thinning



Thin method algorithm & Weight



For particles with $E_i < E_{thin}$

Probability of particle to be kept

$$P_i = E_i / E_M$$

Weight attached to particle

$$W_i = 1 / P_i$$

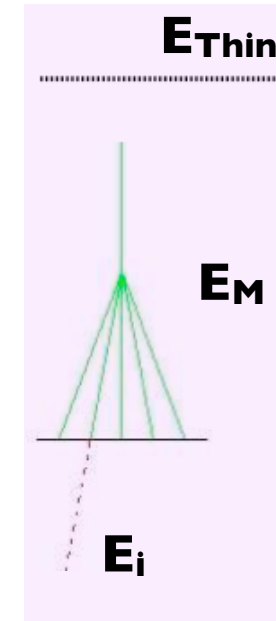
Energy Conservation : ($E_M = E_i * W_i$)

Meaning of Weight!

=particle resembles W_i particles of its kind

Weights are inherited : $W_i' = W_i * W_M$

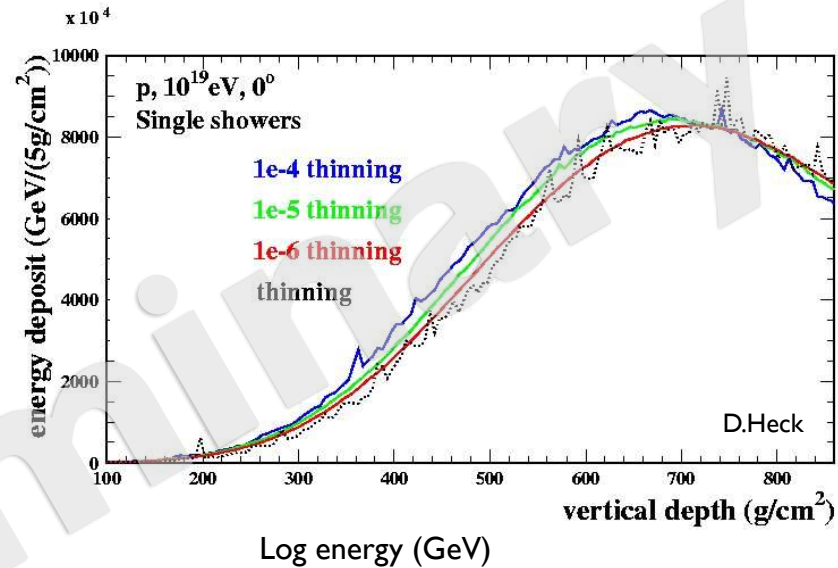
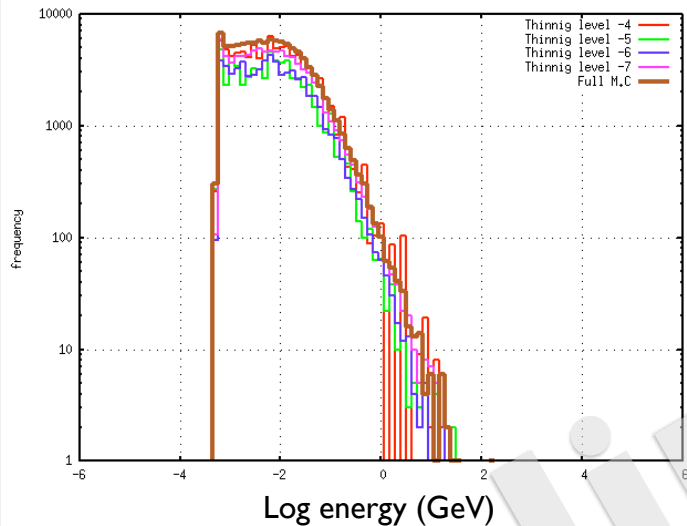
Artificial fluctuations due to weights



Quality of Simulation

ϵ controls **quality** of thinning

Gamma energy distribution at the entire ground



Same seed, random number

Simulation Conditions

$E_0 : 10^{15} \text{eV}$
Primary : Iron
Incident $\theta = 45^\circ$

Fluka&QGSJET-II

Follow all particles with $E_i > E_{\text{thin}}$

$$E_{\text{thin}} = \epsilon * E_0, \quad \epsilon \sim 10^{-4} \sim 10^{-7}$$

ϵ : thinning level

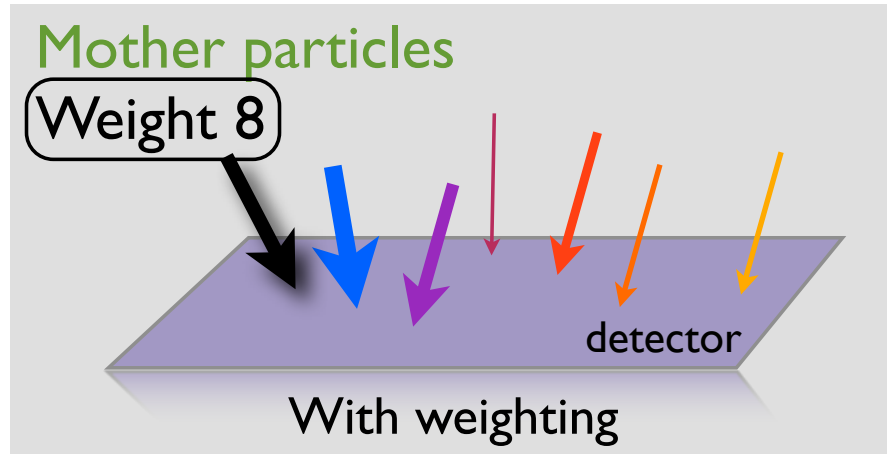
$$W_{\text{max}}(e,g) = \epsilon * E_0 / \text{GeV}$$

$$W_{\text{max}}(m,h) = 0.01 * W_{\text{max}}(e,g)$$

De-thinning

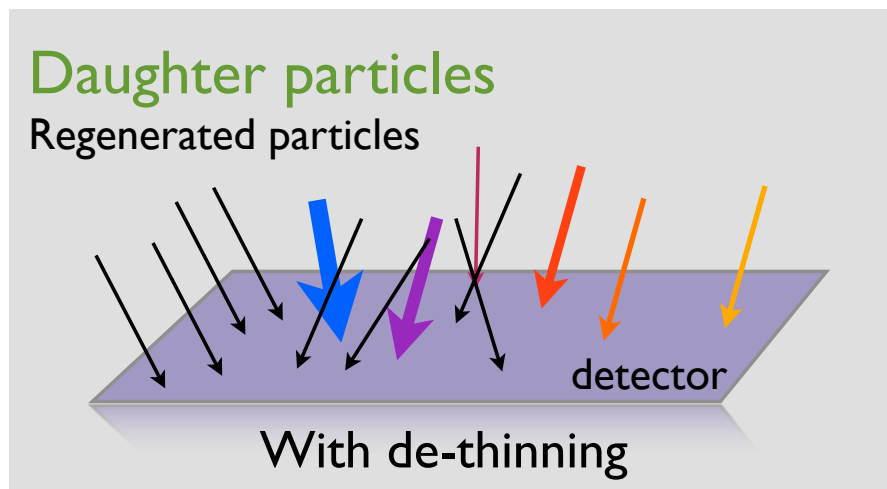
Mother particles

Weight 8



Daughter particles

Regenerated particles



Recorded data

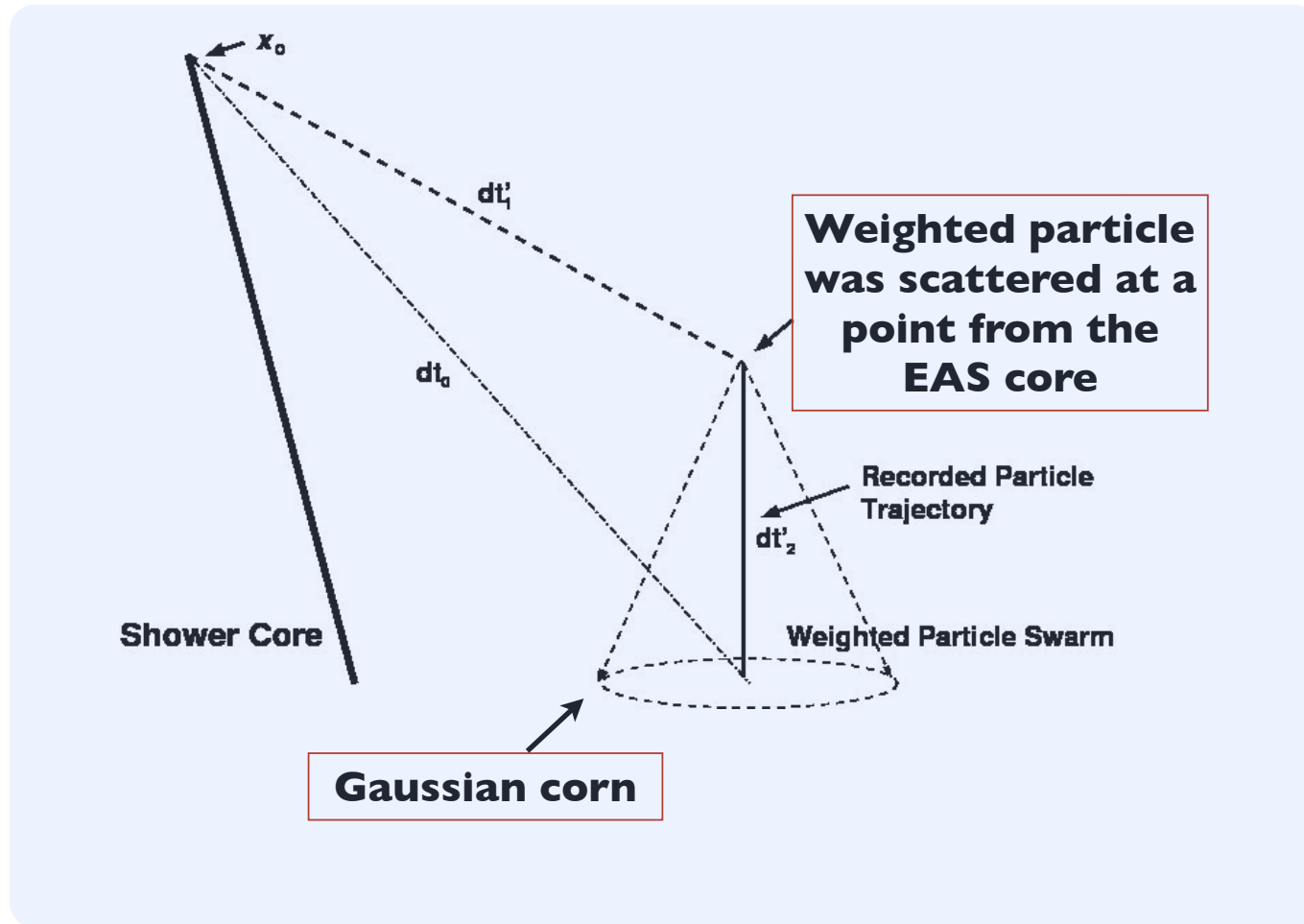
Particle energy
Momentum p_x , p_y , p_z
Position x, y
Incident angle
Incident azimuth angle
Weight

De-thinning

(Keep small fluctuation)

Similar to Full M.C

De-thinning : sprinkle the thinned particles

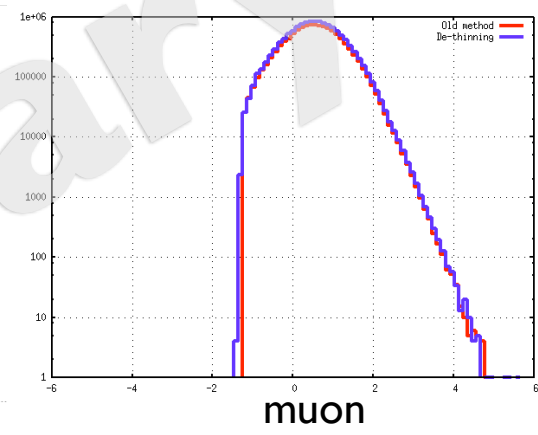
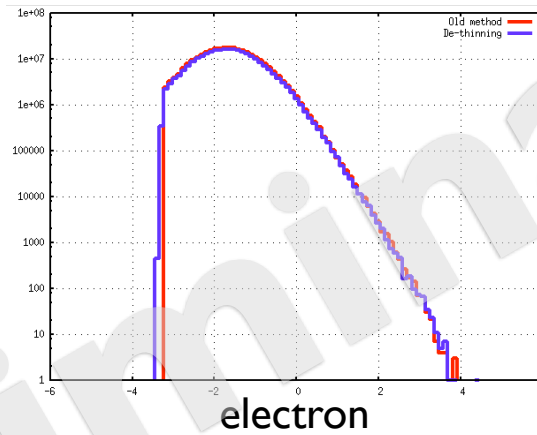
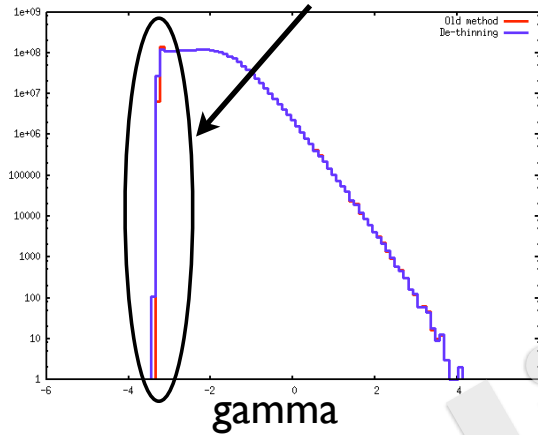


De-thinning results

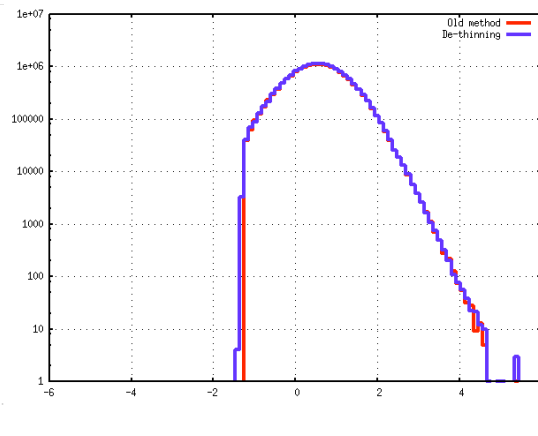
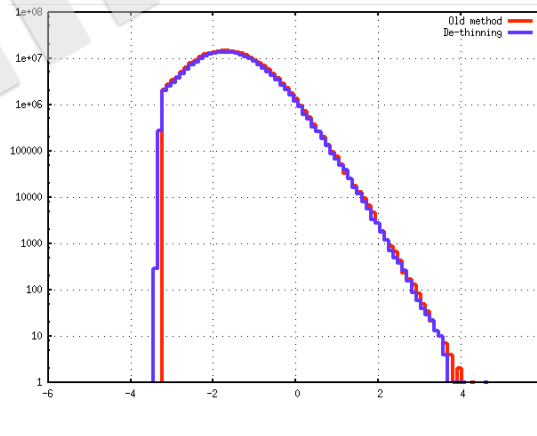
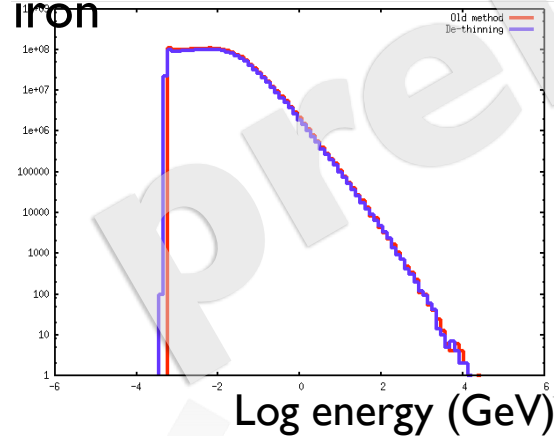
Ground particle spectra recovered based on "weights"

proton

Scatter



iron



Conservation of energy : << 5%

Summary and Conclusions

particle thinning & weight limitation:
technique for M.C simulations at highest energies

$$w_{\max}(e,g) = \varepsilon * E_0/\text{GeV}, \quad w_{\max}(m,h) = w_{\max}(e,g) / 100$$

But, discard produced particles

artificial fluctuations

attach weight to “surviving” particles

De-thinning

Reference

- CORSIKA school : <http://www-ik.fzk.de/corsika/corsika-school2008/participants.htm>
 - B.T. Stokes 2009 ICRC
 - P. Billion 2009, AP 30, 270-285
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